

$\sin 2\beta/\phi_1$ via $b \rightarrow c\bar{c}s$ decays
&
ambiguity removal
via $\cos 2\beta/\phi_1$

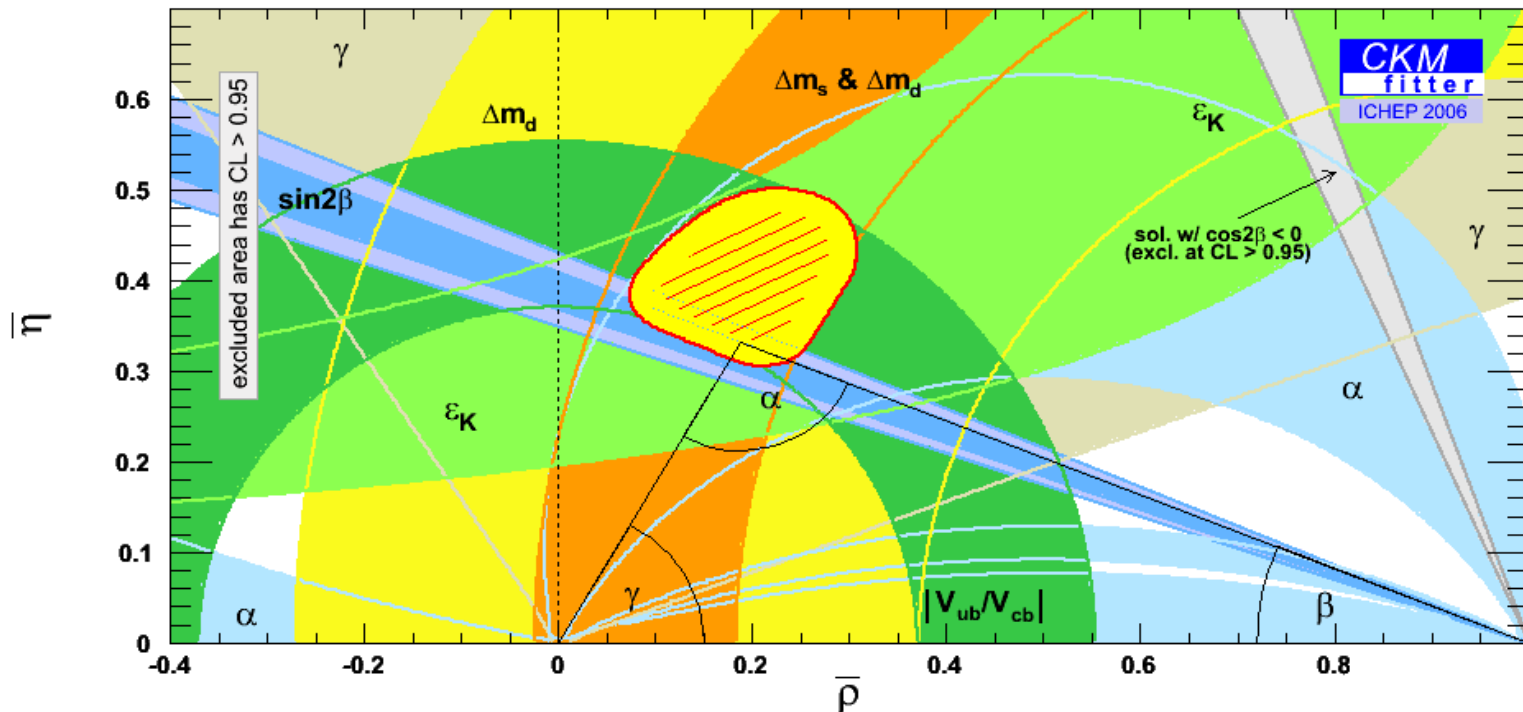
Heiko Lacker, TU Dresden
on behalf of *BABAR* & Belle

BEAUTY 2006, Oxford
September 25, 2006

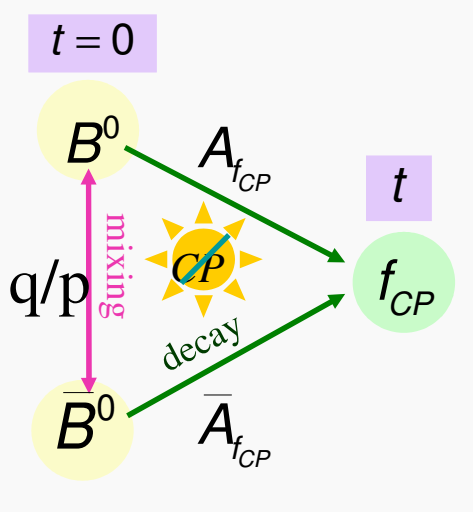


Time-dependent CP asymmetry in $b \rightarrow c\bar{c}s$ decays

- * SM interpretation in terms of $\sin 2\beta$: Theoretically clean ($< O(0.01)$)
- * Experimentally “Easy”
- * Reference for loop-mediated decays (see talk by Y. Ushiroda)
- * Most precise constraint on $\bar{\rho}-\bar{\eta}$
- * Probe NP phase in $B-\bar{B}$ mixing (Constraint almost tangent to $|V_{ub}|$!)



Time-dependent CP-Asymmetries in B_d system



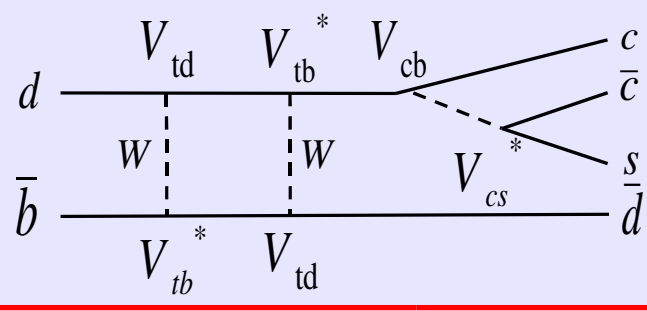
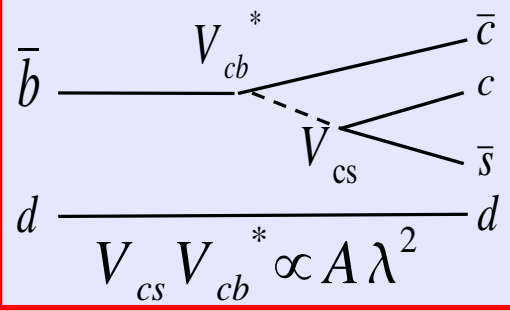
$$A_{CP}(t) = \frac{\Gamma(\bar{B}^0(t) \rightarrow f_{CP}) - \Gamma(B^0(t) \rightarrow f_{CP})}{\Gamma(\bar{B}^0(t) \rightarrow f_{CP}) + \Gamma(B^0(t) \rightarrow f_{CP})}$$

$$\lambda_{f_{CP}} = \eta_{f_{CP}} \frac{q}{p} \frac{\bar{A}_{f_{CP}}}{A_{f_{CP}}}$$

$$= \frac{2 \operatorname{Im} \lambda}{1 + |\lambda|^2} \sin(\Delta m_d t) - \frac{1 - |\lambda|^2}{1 + |\lambda|^2} \cos(\Delta m_d t)$$

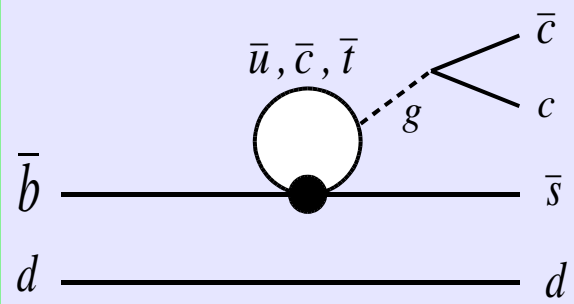
\parallel
 S $=$ $-A$ (*Belle*) $=$ C (*BABAR*)

$B^0 / \bar{B}^0 \rightarrow (c \bar{c}) K_{CP}^0$ (e.g. $\rightarrow \pi^+ \pi^-$)



$$\frac{q}{p} \frac{\bar{A}}{A} \approx e^{-2 \cdot i \beta}$$

$$\frac{q}{p} \approx \frac{V_{tb}^* V_{td}}{V_{tb} V_{td}^*}$$



$$V_{cs} V_{cb}^* \propto A \lambda^2$$

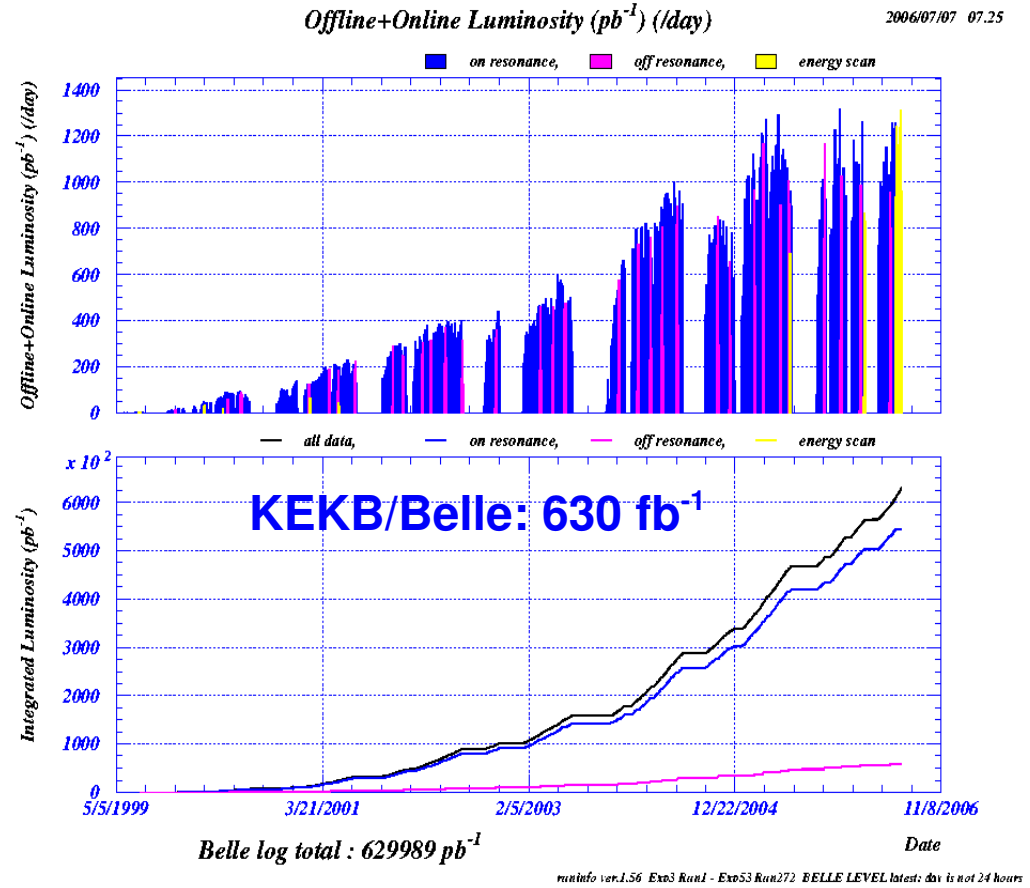
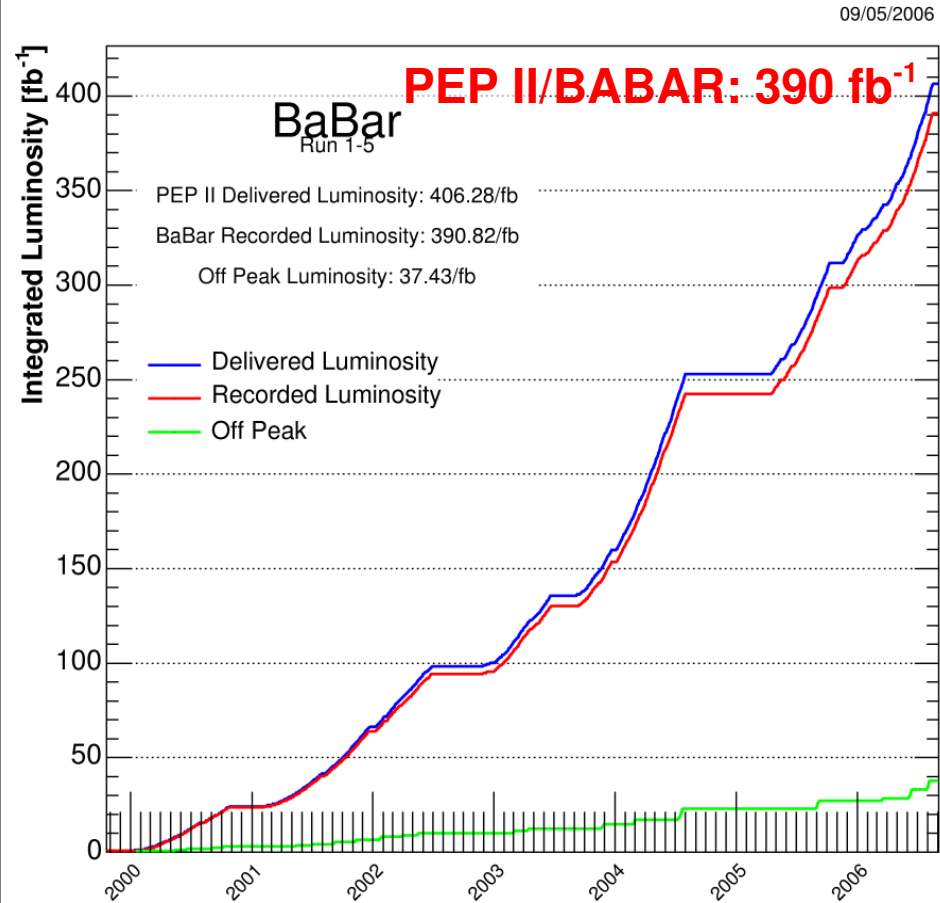
$$V_{ts} V_{tb}^* \propto A \lambda^2$$

$$V_{us} V_{ub}^* \propto A \lambda^4$$

To a very good approximation:

$$A_{CP}(t) = \sin(2\beta) \cdot \sin(\Delta m_d t)$$

The B-factories have passed 1 ab⁻¹



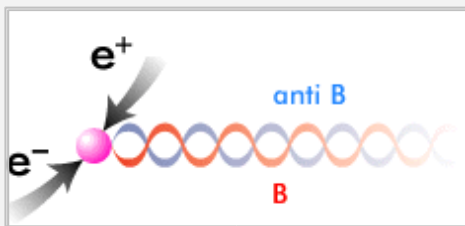
Luminosity Records (10³⁴ cm⁻² s⁻¹)

KEKB: 1.6517 (June 29, 2006)

PEP II: 1.207 (August 16, 2006)

Time-dependent CP violation at the $\Upsilon(4S)$

Coherent State

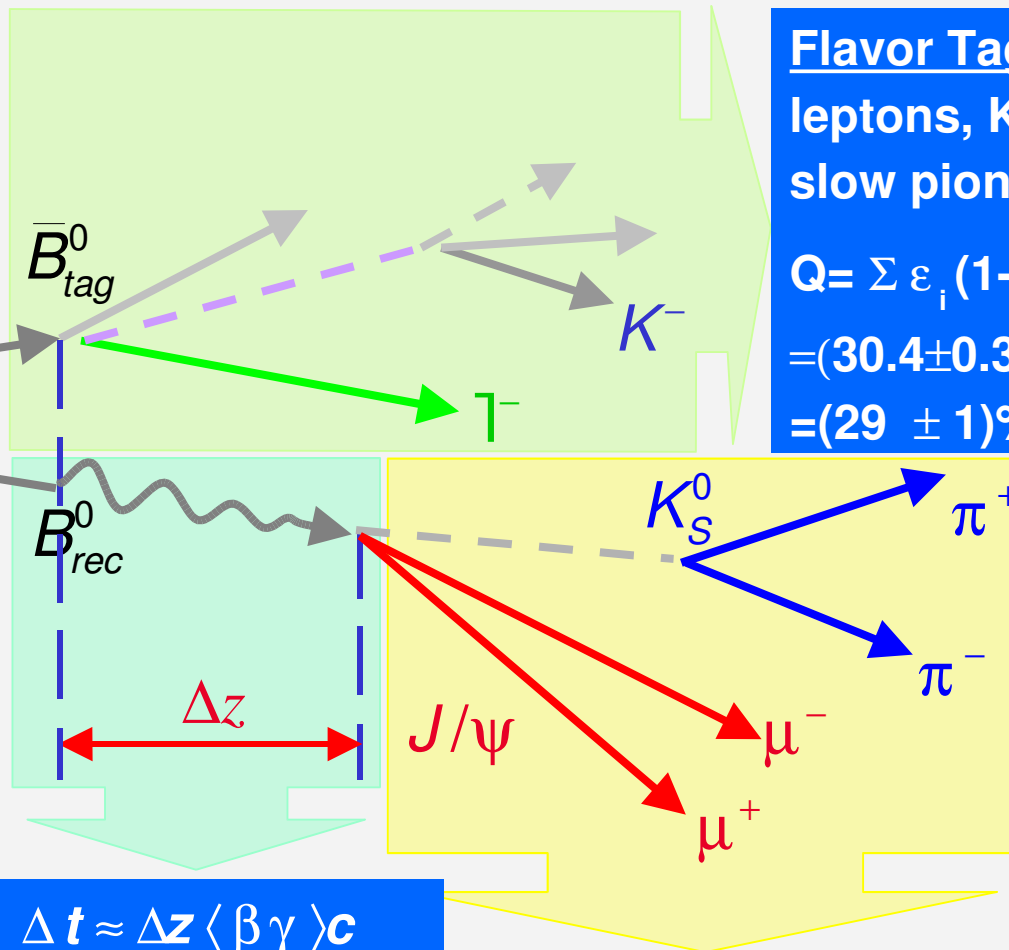


$\Upsilon(4S)$

$e^- \rightarrow \Upsilon(4S) \leftarrow e^+$

9 GeV BABAR/PEPII 3.1 GeV
8 GeV Belle/KEKB 3.5 GeV

$\beta\gamma = 0.56$ (BABAR)
 $= 0.425$ (Belle)



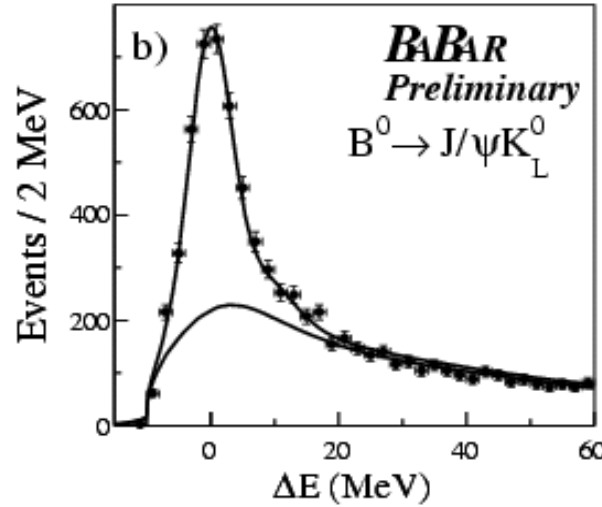
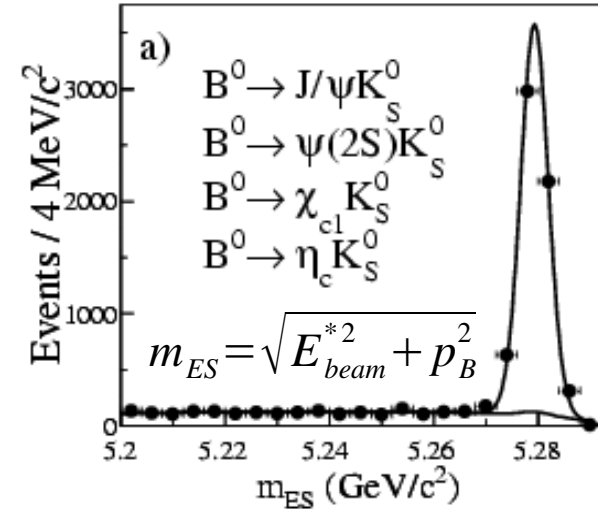
Flavor Tagging
leptons, Kaons,
slow pions from D^*

$Q = \sum \varepsilon_i (1 - 2w_i)^2$
 $= (30.4 \pm 0.3)\%$ (BABAR)
 $= (29 \pm 1)\%$ (Belle)

$\Delta t \approx \Delta z \langle \beta\gamma \rangle c$
 $\langle \Delta z \rangle \approx 250 \mu\text{m}$ (BABAR)
 $\approx 200 \mu\text{m}$ (Belle)
 $\sigma(\Delta z) \approx 190 \mu\text{m}$

Exclusive B-meson reconstruction:
e.g. CP Eigenstate

BABAR (hep-ex/0607107): 348 M $B\bar{B}$



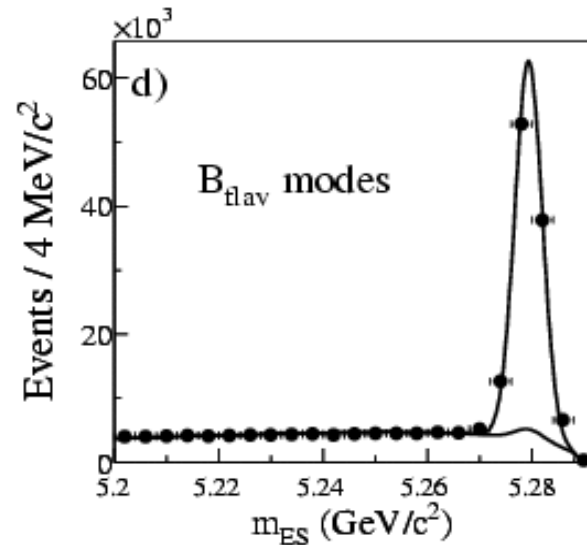
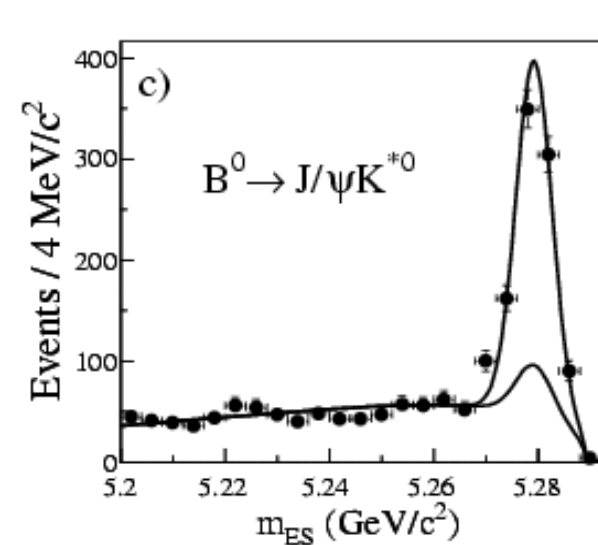
$$B \rightarrow (c\bar{c}) K_S^0 \quad \eta_{CP} = -1$$

$$J/\Psi \rightarrow e^+ e^-, \mu^+ \mu^-$$

$$\Psi(2S) \rightarrow e^+ e^-, \mu^+ \mu^-; J/\Psi \pi^+ \pi^-$$

$$\chi_{c1} \rightarrow J/\Psi \gamma \quad \eta_c \rightarrow K_S K^+ \pi^-$$

$$K_S \rightarrow \pi^+ \pi^-, (\pi^0 \pi^0)$$



$$B \rightarrow J/\Psi K^{*0} \quad K^{*0} \rightarrow K_S \pi^0$$

VV-mode => admixture of CP-odd/CP-even final states

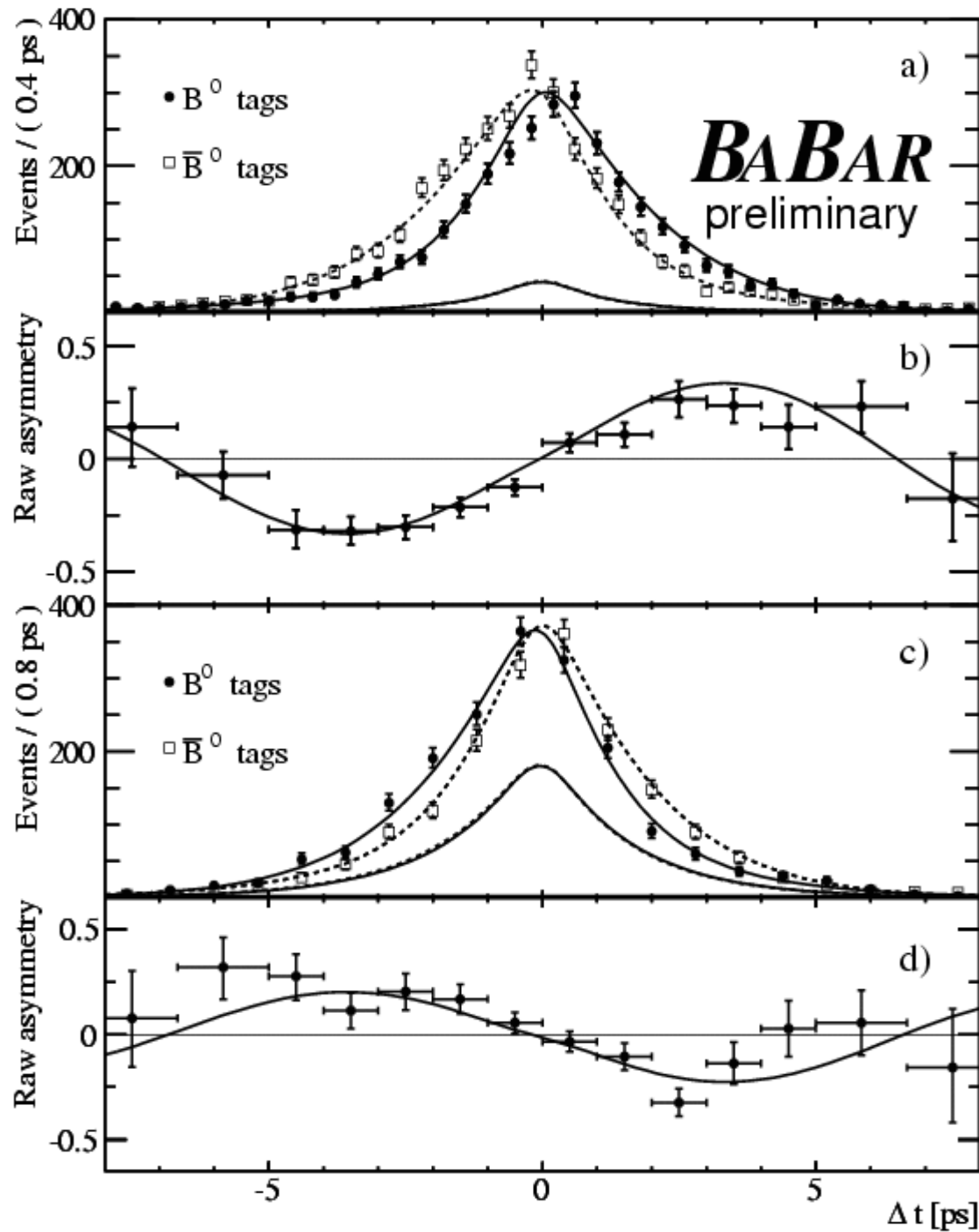
Angular analysis: $\eta_{CP} = 0.504$
(hep-ex/0607081)

$$B \rightarrow J/\Psi K_L^0 \quad K_L \text{-energy not measured!} \quad \eta_{CP} = +1$$

Apply kinematic constraint: $M_B^2 = (p_{J/\Psi} + p_{K_L})^2$

Remaining degree of freedom: $\Delta E = E_{J/\Psi}^* + E_{K_L}^* - E_{beam}^*$

$\sin 2\beta$: *BABAR* Results



CP odd: $\eta_{CP} = -1$ $B \rightarrow (c\bar{c})K_S^0$

$$\sin 2\beta = +0.713 \pm 0.038$$

$$C = -A = +0.070 \pm 0.028 \pm 0.018$$

CP even: $\eta_{CP} = +1$ $B \rightarrow J/\Psi K_L^0$

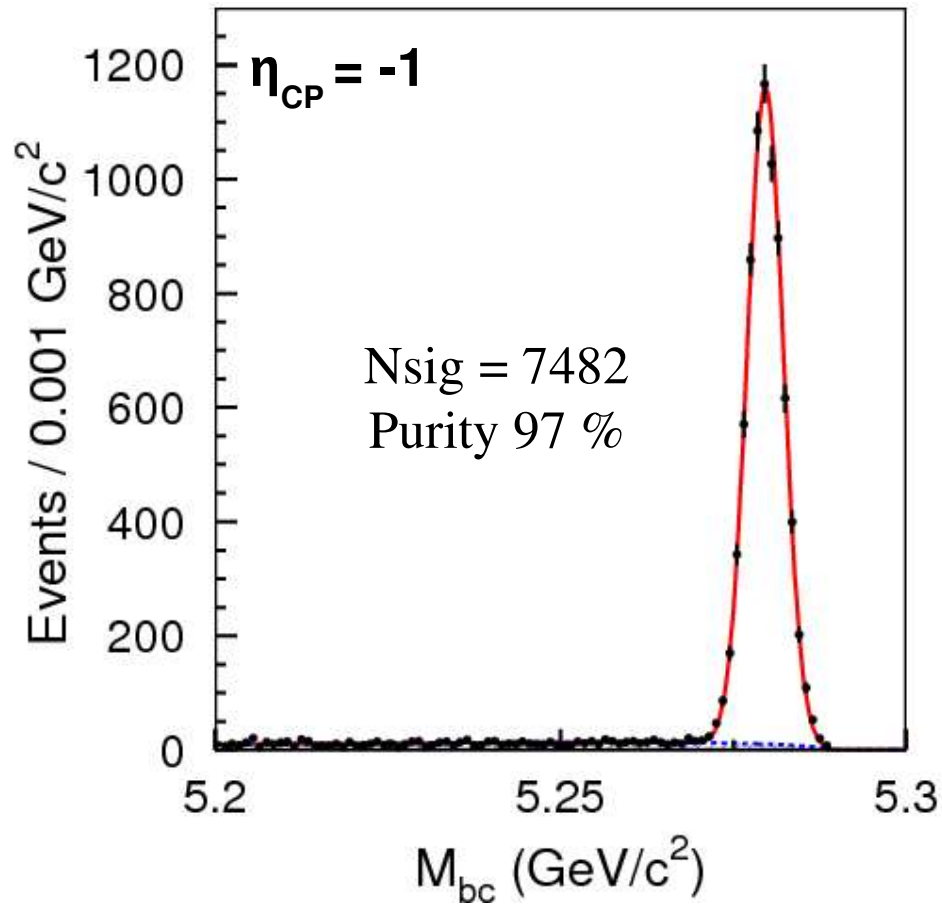
$$\sin 2\beta = +0.716 \pm 0.080$$

Full CP sample:

$$\sin 2\beta = +0.710 \pm 0.034 \pm 0.019$$

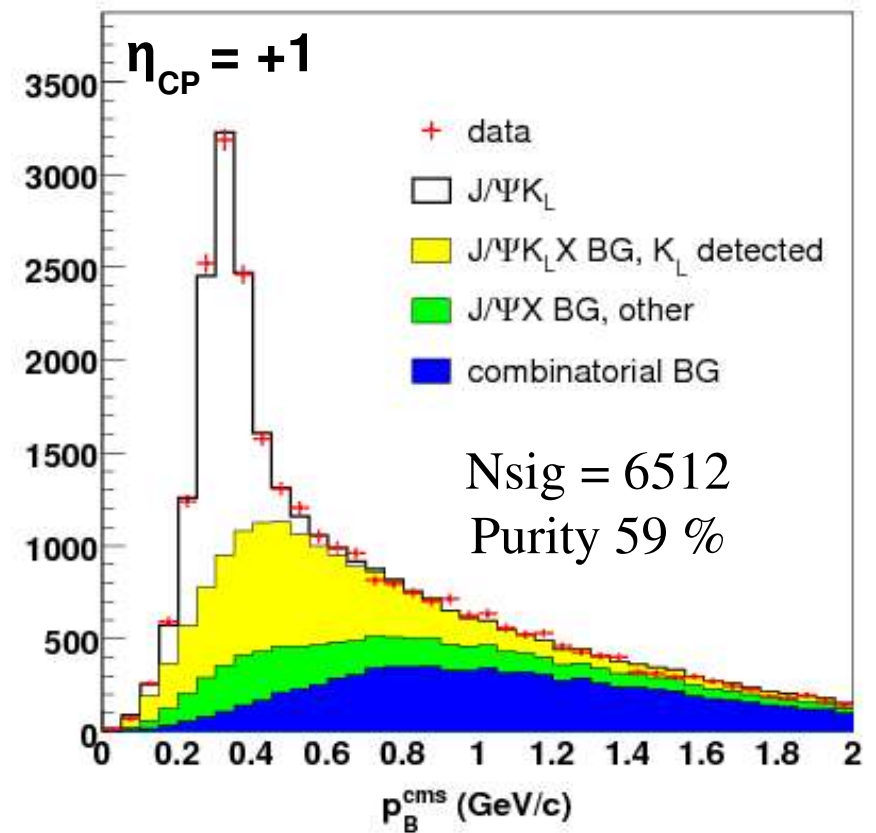
Belle (hep-ex/0608039): 532 M $B\bar{B}$

$$B \rightarrow J/\Psi K_S^0$$



$$M_{bc} = \sqrt{E_{beam}^{*2} - P_{J/\psi K_S}^{*2}}$$

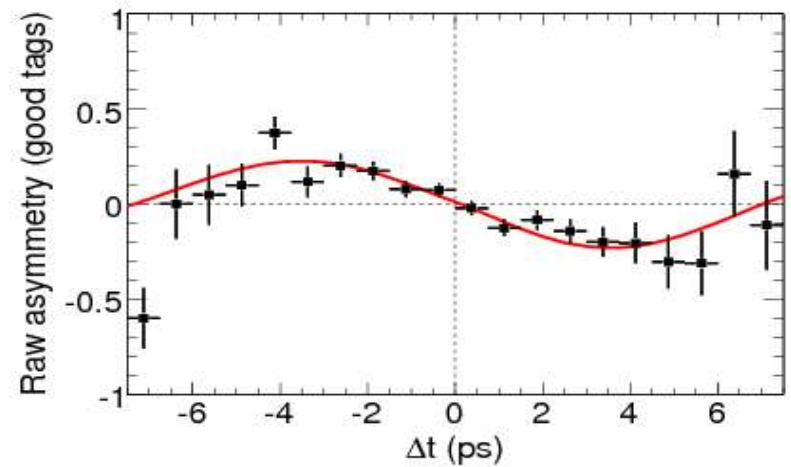
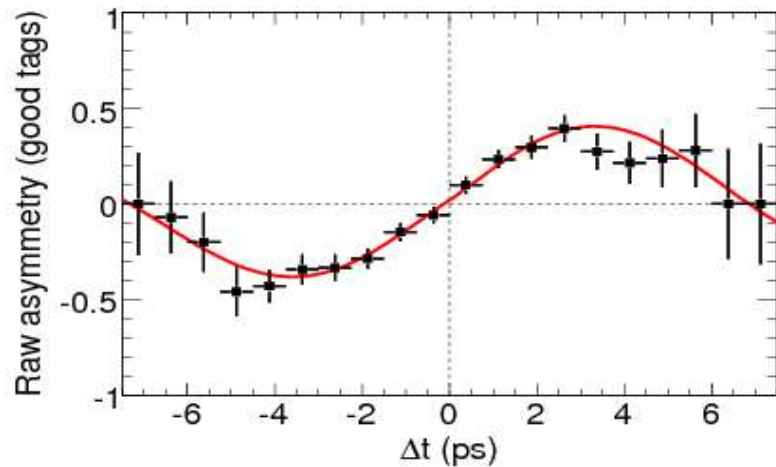
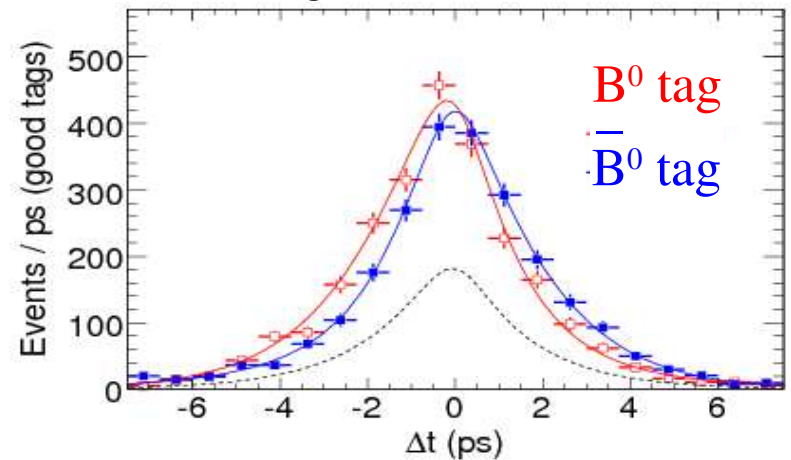
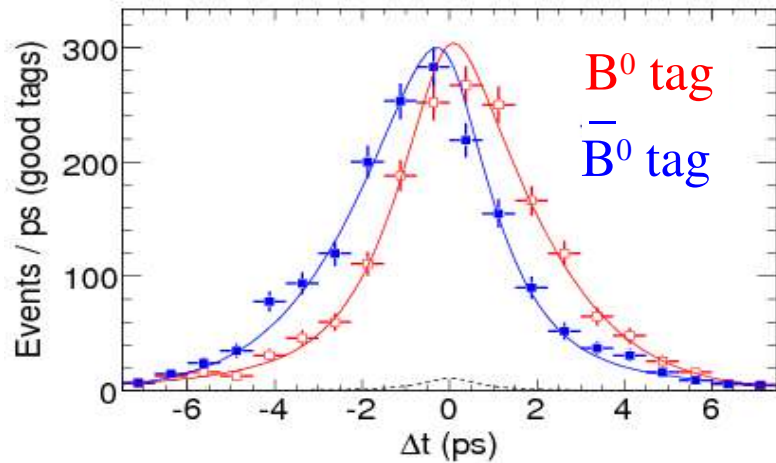
$$B \rightarrow J/\Psi K_L^0$$



sin2β: Belle Results

CP odd: $\eta_{CP} = -1$ $B \rightarrow J/\Psi K_S^0$

CP even: $\eta_{CP} = +1$ $B \rightarrow J/\Psi K_L^0$



$$\sin 2\beta = +0.643 \pm 0.038$$

$$C=-A = 0.001 \pm 0.028$$

$$\sin 2\beta = +0.641 \pm 0.057$$

$$C=-A = -0.045 \pm 0.033$$

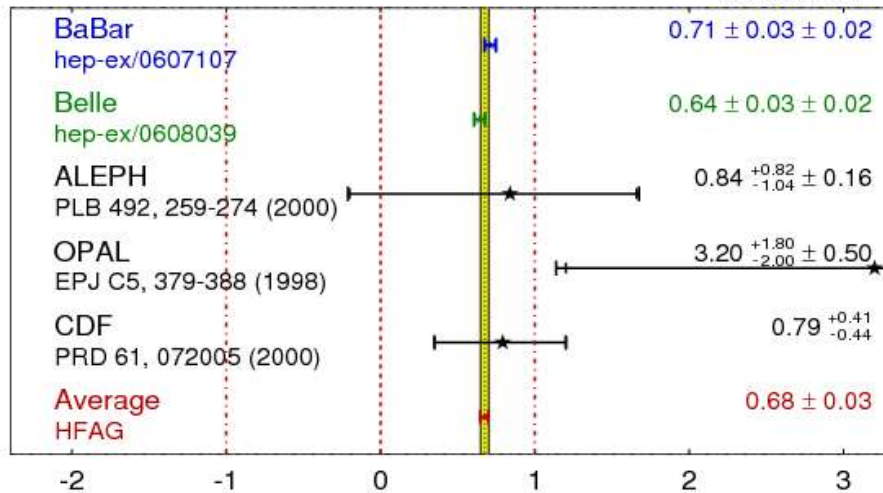
Average

$$\sin 2\beta = +0.642 \pm 0.031 \pm 0.017$$

$$C=-A = -0.018 \pm 0.021 \pm 0.014$$

sin2β: World Average

sin(2β) ≡ sin(2φ₁) **HFAG**
ICHEP 2006
PRELIMINARY

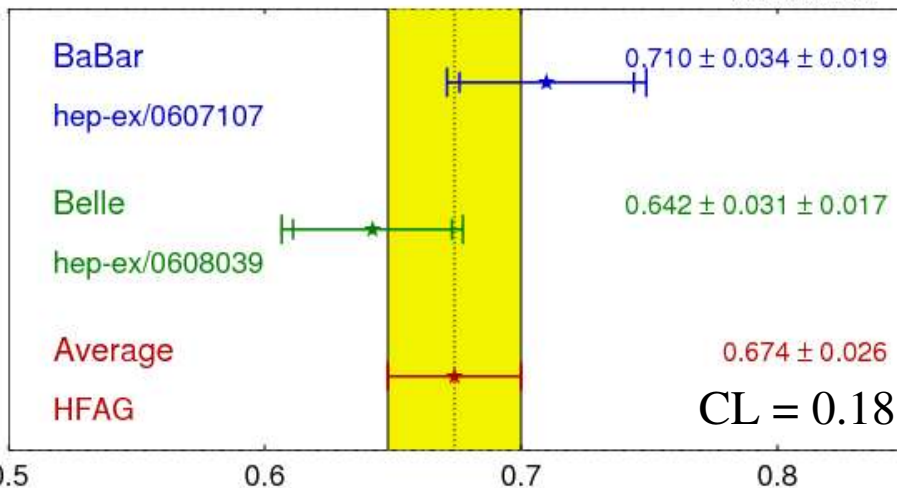


sin(2β) ≡ sin(2φ₁) (All charmonium):
0.675 ± 0.023_{stat} ± 0.012_{sys} (CL = 0.36)

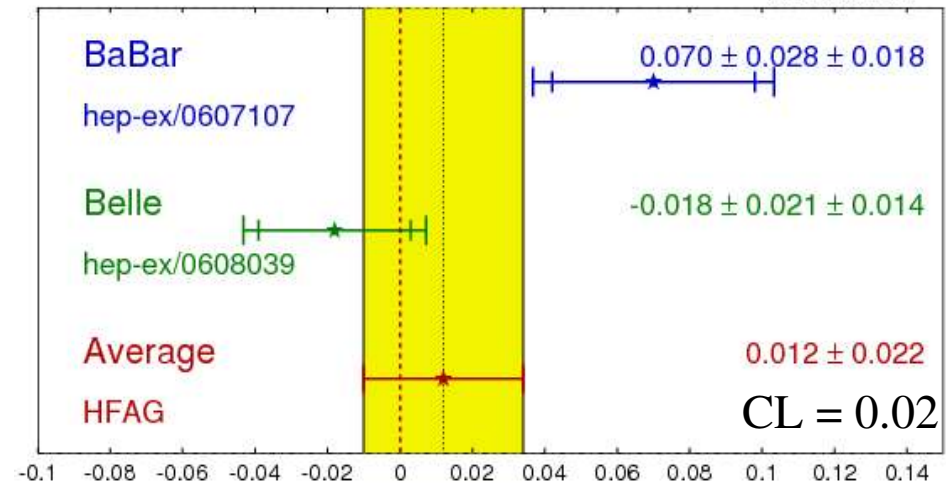
Solutions for β ≡ φ₁ (in [0, π]) :
β ≡ φ₁ = (21.2 ± 1.0)° or (68.8 ± 1.0)°

B-Factories only

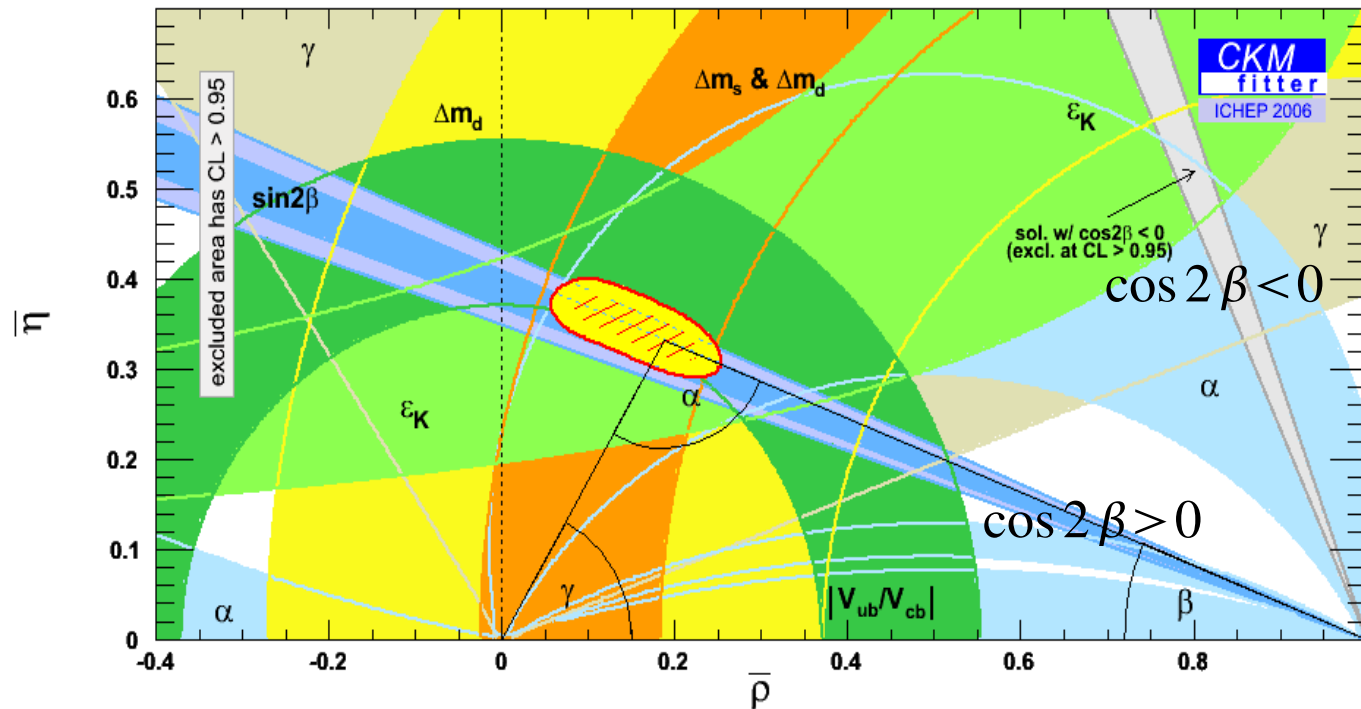
sin(2β) ≡ sin(2φ₁) **HFAG**
ICHEP 2006
PRELIMINARY



b → ccs C_{CP} **HFAG**
ICHEP 2006
PRELIMINARY



$\sin 2\beta$: Interpretation



Do we have to care about the $\cos 2\beta < 0$ solution?

**Yes: In the presence of New Physics in B-mixing
we are measuring $\sin(2\beta + 2\Theta_d)$ instead of $\sin(2\beta)$**

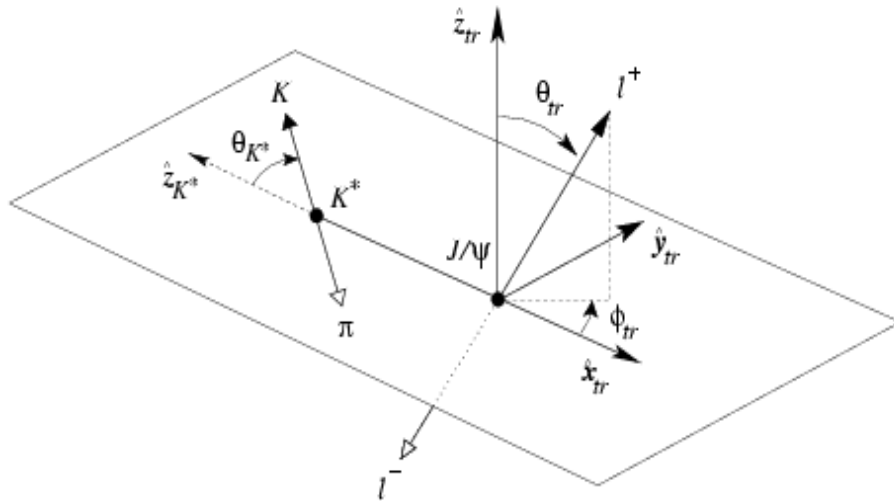
**Consequence: $\cos 2\beta < 0$ solution is not excluded as long
as the sign has not been measured**

$\cos 2\beta$ from $B \rightarrow J/\psi K^*$

Transversity base to describe differential decay rate:

$$\vec{\omega} = (\theta_{K^*}, \theta_{tr}, \phi_{tr})$$

$$\vec{A} = (|A_0|e^{i\delta_0}, |A_{\parallel}|e^{i\delta_{\parallel}}, |A_{\perp}|e^{i\delta_{\perp}})$$



Problem: Strong phase ambiguity

$$(\delta_{\parallel} - \delta_0, \delta_{\perp} - \delta_0, \cos 2\beta) \Leftrightarrow (\delta_0 - \delta_{\parallel}, \pi + \delta_0 - \delta_{\perp}, -\cos 2\beta)$$

BABAR 88 $M B \bar{B}$

PRD 71, 032005 (2005)

$$\sin 2\beta = 0.10 \pm 0.57 \pm 0.14_{\text{sys}} \quad \cos 2\beta = 2.72^{+0.50}_{-0.79} \pm 0.27$$

$$\cos 2\beta = 3.32^{+0.76}_{-0.96} \pm 0.27_{\text{sys}} \quad \text{if } \sin 2\beta \equiv 0.731$$

$\cos 2\beta > 0$ @ 87% CL

Sign ambiguity resolved using S-P interference in $K\pi$ system

Belle 275 $M B \bar{B}$

PRL 95, 091601 (2005)

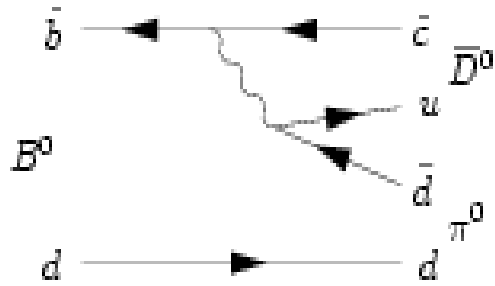
$$\sin 2\beta = 0.24 \pm 0.31 \pm 0.05_{\text{sys}} \quad \cos 2\beta = 0.87 \pm 0.74 \pm 0.12$$

$$\cos 2\beta = 0.56 \pm 0.79 \pm 0.11_{\text{sys}} \quad \text{if } \sin 2\beta \equiv 0.726$$

Belle chooses solution as expected from s-quark helicity conservation (M. Suzuki, Phys. Rev. D 64, 117503 (2001)) in agreement with the sign found in BABAR's analysis.

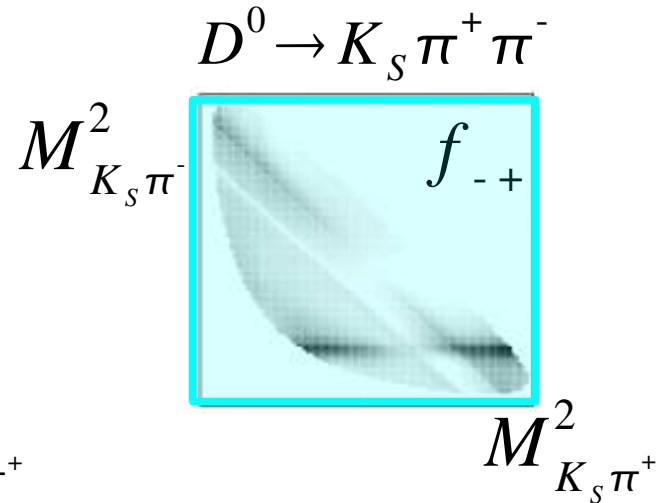
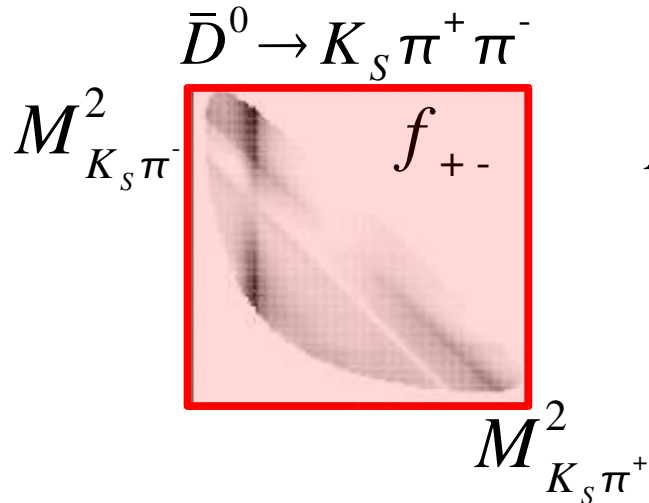
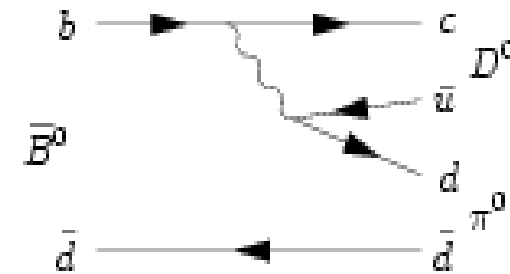
cos2β from B → D⁰/D̄⁰ h⁰

A. Bondar, T. Gershon and P. Krokovny, PLB 624, 1 (2005)



Amplitudes interference like in the Dalitz method to extract γ:

$$D^0/\bar{D}^0 \rightarrow K_S \pi^+ \pi^-$$



Amplitudes (no (direct) CP violation in B & D system):

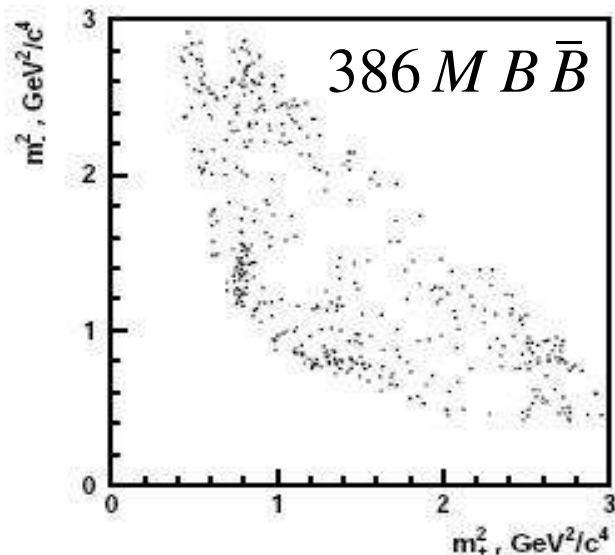
$$M_{\bar{B}^0}(t) = f_{-+} \cos(\Delta m t/2) - i e^{-i2\beta} \eta_{h^0} (-1)^l f_{+-} \sin(\Delta m t/2)$$

$$M_{B^0}(t) = f_{+-} \cos(\Delta m t/2) - i e^{+i2\beta} \eta_{h^0} (-1)^l f_{-+} \sin(\Delta m t/2)$$

η_{h^0} : CP Eigenvalue, $l=l(D h^0)$ f_{+-}, f_{-+} known $\Rightarrow \sin 2\beta$ & $\cos 2\beta$

cos2β from B → D⁰/ \bar{D}^0 h⁰

Belle PRL 97, 081801 (2006)



Final state	sin 2φ ₁	cos 2φ ₁
Dπ ⁰ , Dη[γγ]	0.80 ^{+0.54} _{-0.60}	2.07 ^{+0.78} _{-0.91}
Dω, Dη[3π]	0.43 ± 0.90	1.53 ^{+0.67} _{-0.93}
D*π ⁰ , D*η	1.07 ± 1.14	3.46 ^{+1.80} _{-2.01}
Simultaneous fit	0.78 ± 0.44	1.87 ^{+0.40} _{-0.53}

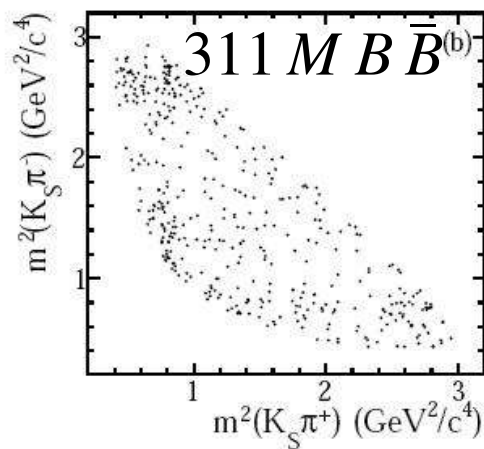
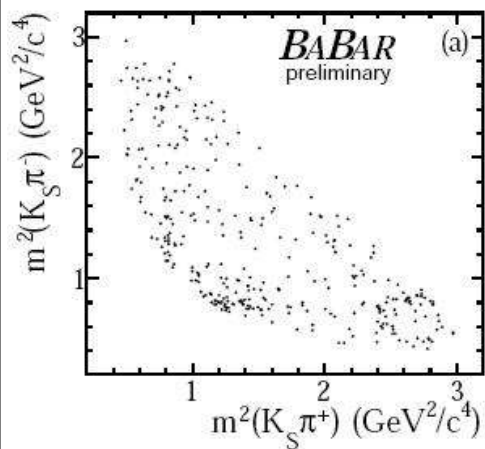
$$\sin 2\beta = 0.78 \pm 0.44 \pm 0.22_{\text{sys} + \text{Dalitz}}$$

$$\cos 2\beta > 0$$

$$\cos 2\beta = 1.87^{+0.40+0.22}_{-0.53-0.32} (\text{sys} + \text{Dalitz})$$

$$@ 98.3\% \text{ CL}$$

BABAR hep-ex/0607105



Final state	cos 2β	sin 2β	λ
D ⁰ π ⁰	1.1 ^{+0.8} _{-0.9}	1.0 ± 0.5	1.13 ^{+0.17} _{-0.14}
D ⁰ η ^(r)	0.4 ± 1.1	-0.1 ^{+0.9} _{-1.0}	0.96 ^{+0.19} _{-0.16}
D ⁰ ω	-0.4 ^{+1.3} _{-1.4}	0.7 ± 1.0	0.61 ^{+0.17} _{-0.15}
D* ⁰ π ⁰ /η	0.3 ± 1.4	-0.8 ^{+1.0} _{-0.9}	1.05 ^{+0.35} _{-0.25}
All	0.54 ± 0.54	0.45 ± 0.35	0.98 ± 0.09
All	0.55 ± 0.52	0.685 (fixed)	1 (fixed)

$$\sin 2\beta = 0.45 \pm 0.36 \pm 0.05_{\text{sys}} \pm 0.07_{\text{Dalitz}}$$

$$\cos 2\beta > 0$$

$$\cos 2\beta = 0.54 \pm 0.54 \pm 0.08_{\text{sys}} \pm 0.18_{\text{Dalitz}}$$

$$@ 87\% \text{ CL}$$

cos2β from $B^0/\bar{B}^0 \rightarrow D^{*+} D^{*-} K_S$

T.E. Browder, A. Datta, P.J O'Donnell and S. Pakvasa, PRD 61, 054009 (2000)

$$A_{CP}(t; \sin 2\beta, \cos 2\beta) = \eta_y \frac{J_c}{J_0} \cos(\Delta m_d t) - \left(\frac{2J_{s1}}{J_0} \sin 2\beta + \eta_y \frac{2J_{s2}}{J_0} \cos 2\beta \right) \sin(\Delta m_d t)$$

$$\eta_y = -1 (+1) \text{ for } s^+ \geq s^- (s^+ \leq s^-)$$

$$s^+ = m^2(D^{*+} K_S), s^- = m^2(D^{*-} K_S)$$

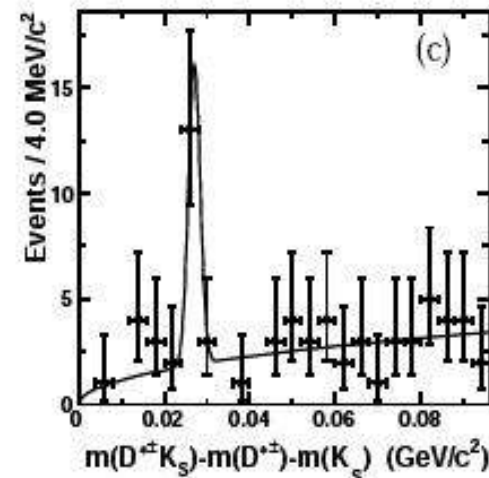
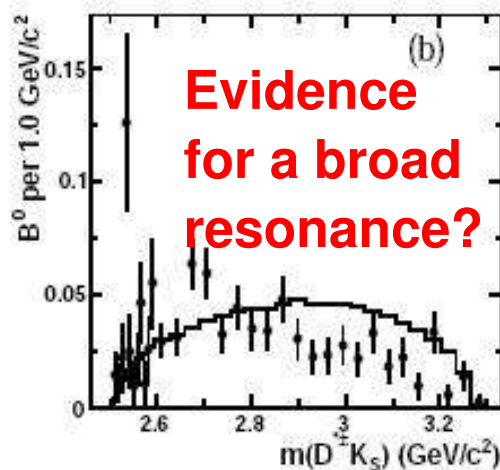
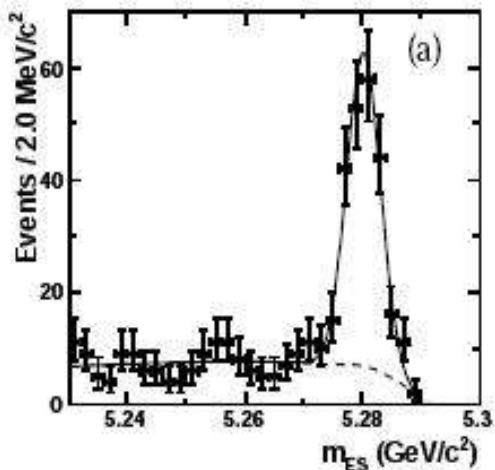
$$J_0 = \int_{s^+ < s^-} (|A|^2 + |\bar{A}|^2) ds, \quad J_c = \int_{s^+ < s^-} (|A|^2 - |\bar{A}|^2) ds$$

$$J_{s1} = \int_{s^+ < s^-} \Re(\bar{A} A^*) ds, \quad J_{s2} = \int_{s^+ < s^-} \Im(\bar{A} A^*) ds$$

Can be large if a (broad) intermediate resonant state contributes

BABAR hep-ex/0608016 (preliminary)

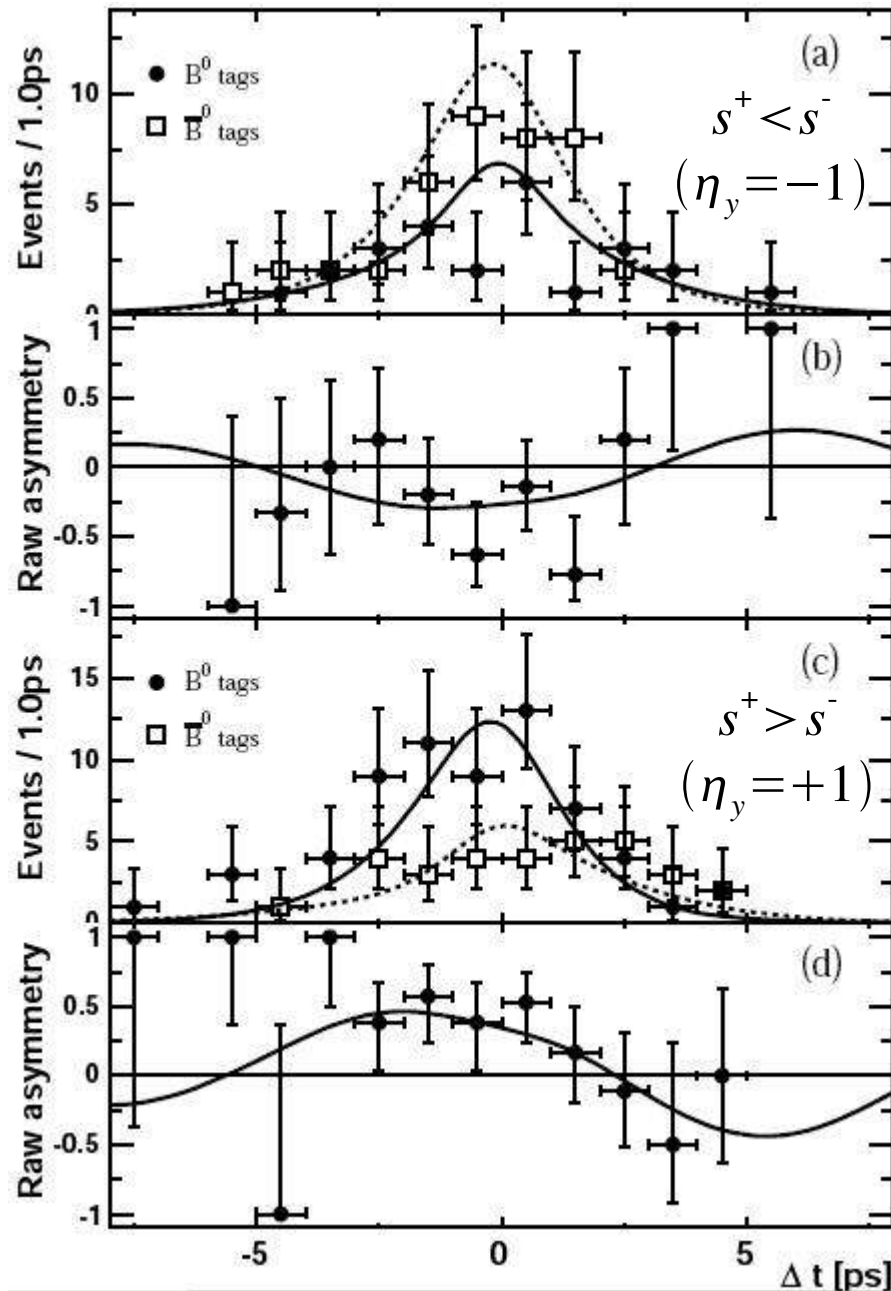
230 M $B\bar{B}$



$\cos 2\beta$ from $B^0/\bar{B}^0 \rightarrow D^{*+} D^{*-} K_S$

BABAR hep-ex/0608016 (preliminary)

230 $M B \bar{B}$



Fit results:

$$\frac{J_c}{J_0} = 0.76 \pm 0.18(\text{stat}) \pm 0.07(\text{syst})$$

$$\frac{2J_{s1}}{J_0} \sin 2\beta = 0.10 \pm 0.24(\text{stat}) \pm 0.06(\text{syst})$$

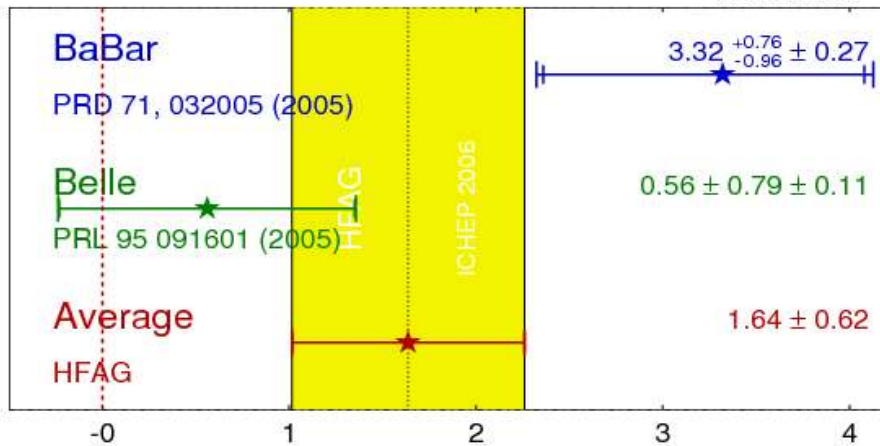
$$\frac{2J_{s2}}{J_0} \cos 2\beta = 0.38 \pm 0.24(\text{stat}) \pm 0.05(\text{syst})$$

$\cos(2\beta) > 0$ @ 94% CL assuming $J_{s2} > 0$

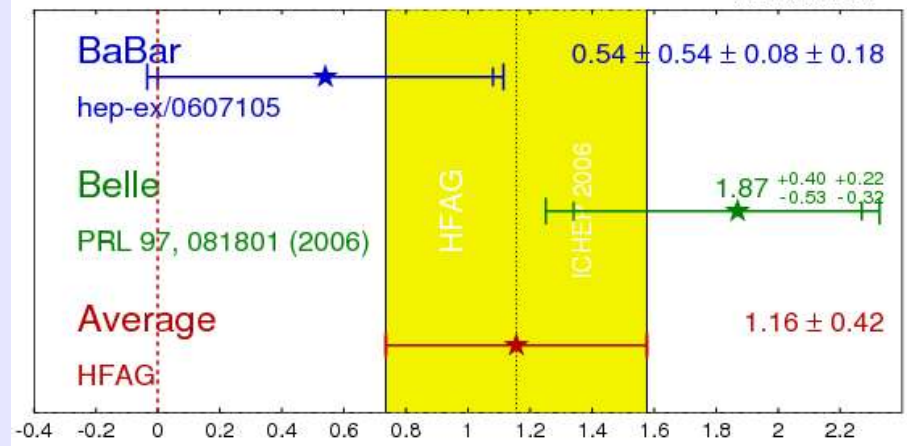
T.E. Browder, A. Datta, P.J O'Donnell
and S. Pakvasa, PRD 61, 054009 (2000)
predict $J_{s2} > 0$.

cos2β: Summary

$$J/\psi K^* \cos(2\beta) \equiv \cos(2\phi_1) \quad \text{HFAG} \\ \text{ICHEP 2006} \\ \text{PRELIMINARY}$$



$$D^{(*)}h^0 \cos(2\beta) \equiv \cos(2\phi_1) \quad \text{HFAG} \\ \text{ICHEP 2006} \\ \text{PRELIMINARY}$$



$B \rightarrow D^* D^* K_s$ (BABAR): $\cos(2\beta) > 0$ @ 94% CL assuming $J_{s2} > 0$

All results prefer $\cos 2\beta > 0 \Rightarrow$ SM solution for β

HFAG: PDG recipe to treat asymmetric errors in the average

“Interpretation of the averages have to be done with greatest care!”

Several results have central values outside the physical region!

Conclusions and Outlook

- * Time-dependent CP asymmetry in $b \rightarrow c\bar{c}s$ provides strongest constraint on $\bar{\rho} - \bar{\eta}$: $\sin(2\beta) = +0.675 \pm 0.023_{\text{stat}} \pm 0.012_{\text{sys}}$
- * $C = -A = -0.018 \pm 0.017 \pm 0.014$ (CL=0.02) consistent with zero
- * Extrapolated $\sin 2\beta$ error (2008): $O(0.02) \leftrightarrow$ Theory: $<O(0.01)$

- * All $\cos 2\beta$ results (BABAR & Belle) consistent with $\cos 2\beta > 0$ (SM):

	BABAR	Belle
$B \rightarrow J/\psi K^*$	@86% CL	-
$B \rightarrow D^0/\bar{D}^0 h^0$	@87% CL	@98.3% CL
$B \rightarrow D^* D^* K_S$	@94% CL	

- * At present: $\cos 2\beta$ average is very difficult to obtain
- * Important constraint on NP phase in $B_d - \bar{B}_d$ mixing