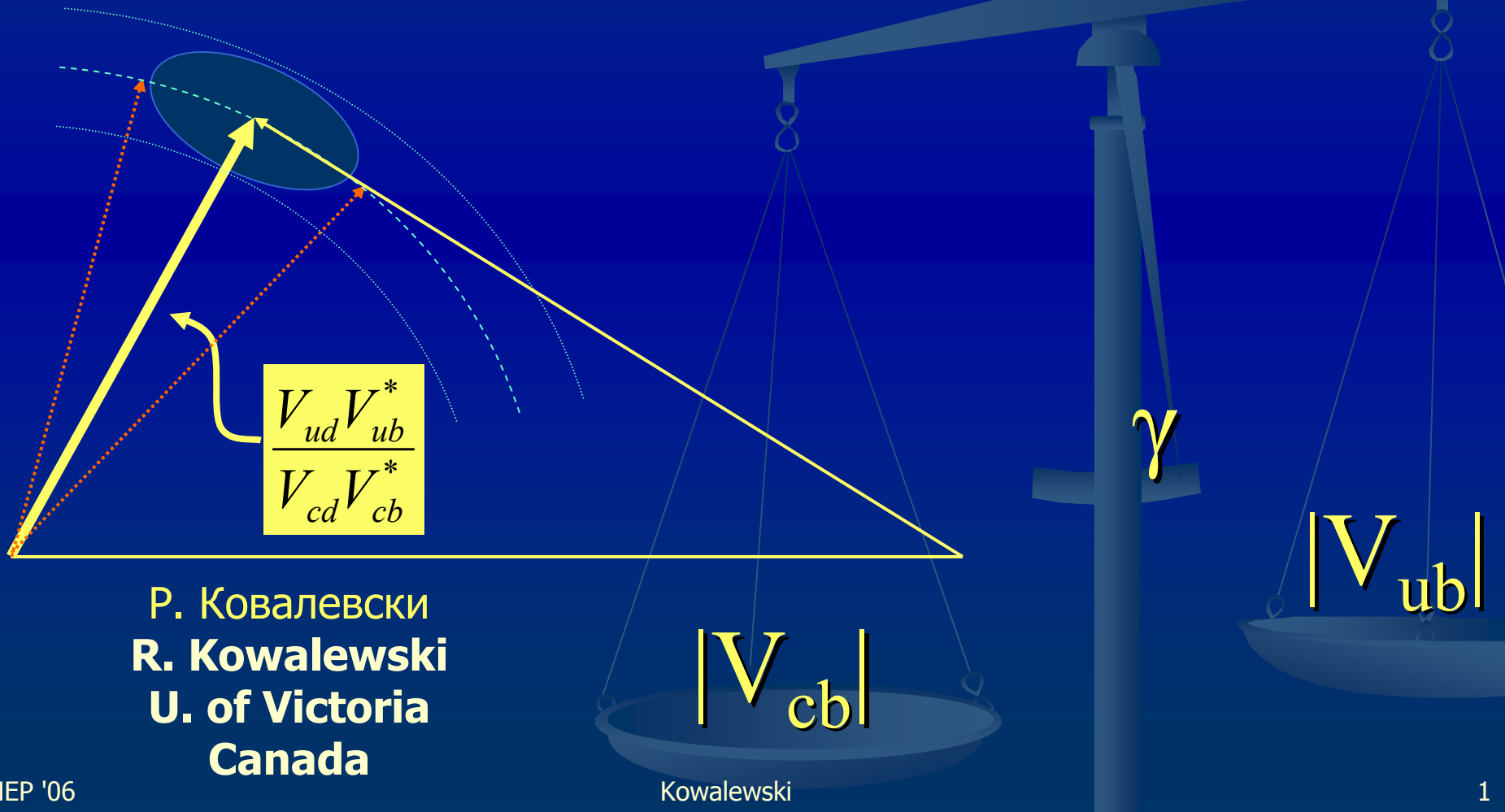


Measuring the apex: $|V_{ub}|$, $|V_{cb}|$ and their relative phase γ (ϕ_3)



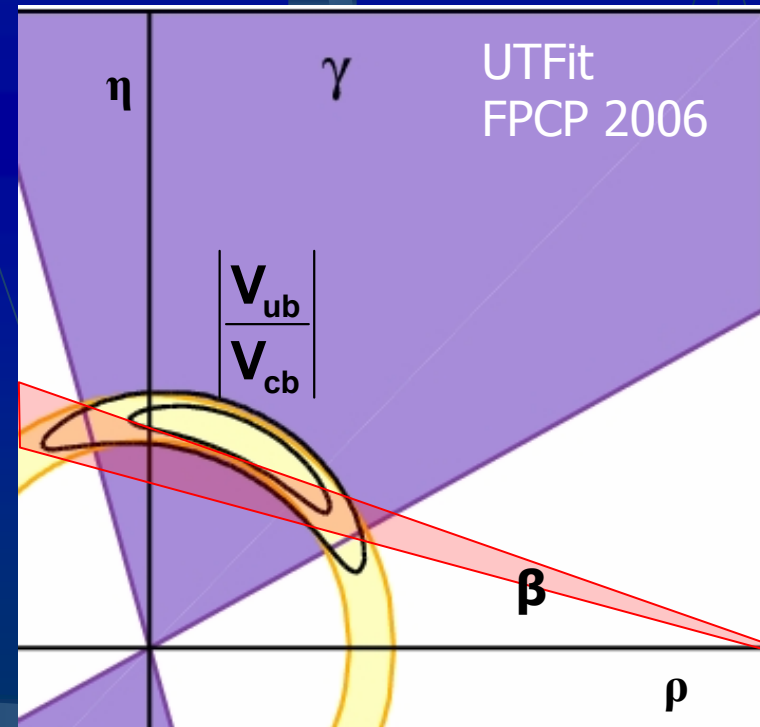
Р. Ковалевски
R. Kowalewski
U. of Victoria
Canada

Kowalewski

Motivation

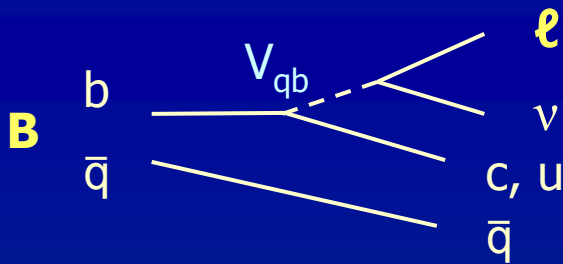
- V_{ub} is a key element of the CKM matrix
- 1 graduate student lifetime (~ 20 years) ago, we didn't know that $V_{ub} \neq 0$:
Was the KM mechanism for $\not{CP}$ viable?
- Now the precise determination of V_{ub} / V_{cb} provides a benchmark for testing new physics in other processes

$$\begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}|e^{-i\gamma} \\ |V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}|e^{-i\beta} & |V_{ts}| & |V_{tb}| \end{pmatrix}$$

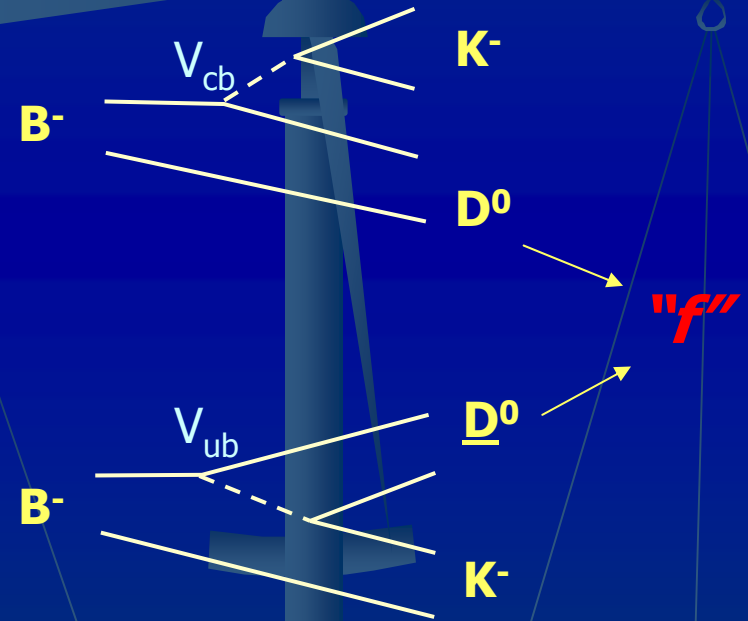


Big trees dominate!

The decay channels used to study $|V_{ub}|$, $|V_{cb}|$ and their relative phase are all dominated by tree diagrams



Lifetime + semileptonic decay determine $|V_{qb}|$



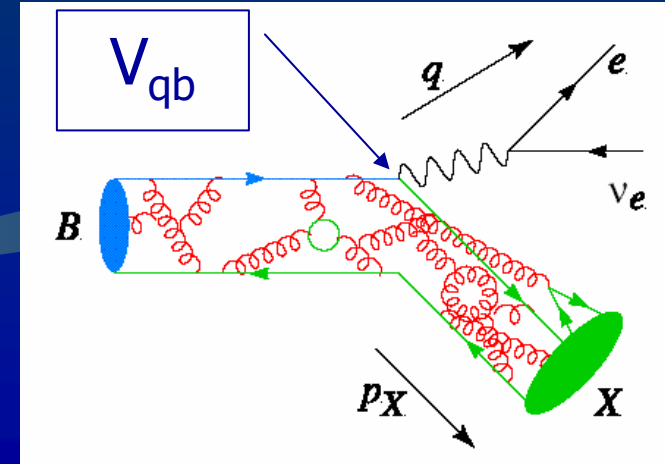
Interference allows phase measurement

$$\begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}|e^{-i\gamma} \\ |V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}|e^{-i\beta} & |V_{ts}| & |V_{tb}| \end{pmatrix}$$

The magnitudes
 $|V_{cb}|$ and $|V_{ub}|$

Semileptonic B decay - theory

- Large BF, only one hadronic current
- Inclusive decays $b \rightarrow q \ell \nu$:
 - Weak quark decay + QCD corrections $\rightarrow$ OPE in α_s and $1/m_b$
- Exclusive decays $B \rightarrow X \ell \nu$:
 - Form factors: need Lattice QCD

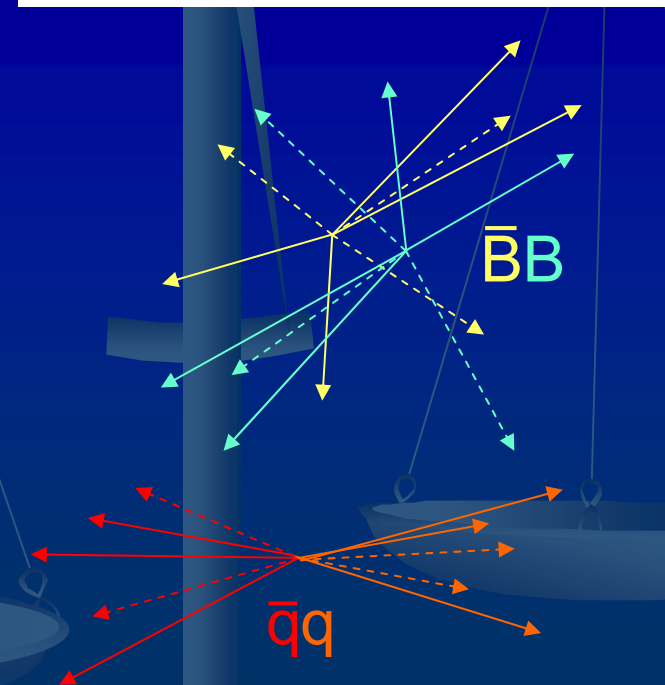
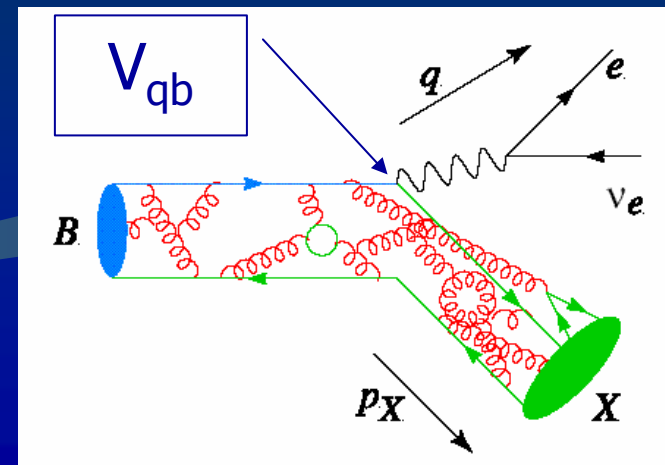


These inclusive and exclusive determinations of V_{qb} are ***complementary***

Semileptonic B decay - experiment



- Inclusive decays $b \rightarrow q\ell\nu$:
 - Measure lepton
 - Measure p_{miss} or associated hadrons
- Exclusive decays $B \rightarrow X_q\ell\nu$:
 - Measure lepton and specified hadrons
- Measurements come from $Y(4S) \rightarrow B\bar{B}$
- Determine non-B contribution using data below $B\bar{B}$ threshold





$$\begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}|e^{-i\gamma} \\ |V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}|e^{-i\beta} & |V_{ts}| & |V_{tb}| \end{pmatrix}$$

Inclusive $|V_{cb}|$

Inclusive decay width

- Total decay width for $b \rightarrow c\ell\nu$:

$$r = m_c / m_b$$

$$\Gamma = |V_{cb}|^2 \frac{G_F^2 m_b^5}{192\pi^3} (1 + A_{ew}) A^{\text{pert}}(r, \mu) \times \left[z_0(r) + \frac{0}{m_b} + z_2\left(r, \frac{\mu_\pi^2}{m_b^2}, \frac{\mu_G^2}{m_b^2}\right) + z_3\left(r, \frac{\rho_D^3}{m_b^3}, \frac{\rho_{LS}^3}{m_b^3}\right) + \dots \right]$$

free quark decay ~ 1.014

Perturbative corrections ~ 0.908

Non-perturbative power corrections

- Similar expressions for $b \rightarrow u\ell\nu$, $b \rightarrow s\gamma$
- Comparison with data relies on quark-hadron duality
 $\rightarrow$ integrate over "broad" regions of phase space

Low-order moments can be calculated reliably



Global fit for $|V_{cb}|$, m_b ...

- Fit predicted moments of inclusive processes $b \rightarrow c l \nu$ and $b \rightarrow s \gamma$ for various cuts on kinematic variables:

$$\left\langle M_x^n \right\rangle_{E_l > E_0} = \tau_B \int_{E_0} M_X^n d\Gamma = f_n^x(E_0, m_b, m_c, \mu_G^2, \mu_\pi^2, \rho_D^3, \rho_{LS}^3)$$

**e or γ
energy cut**

**b-quark
mass**

**c-quark
mass**

**Matrix elements
appearing at order
 $1/m_b^2$ and $1/m_b^3$**

- Calculations available in "kinetic" and "1S" renormalization schemes

Benson, Bigi, Gambino, Mannel, Uraltsev
(several papers)

Bauer, Ligeti, Luke, Manohar, Trott
PRD 70:094017 (2004)

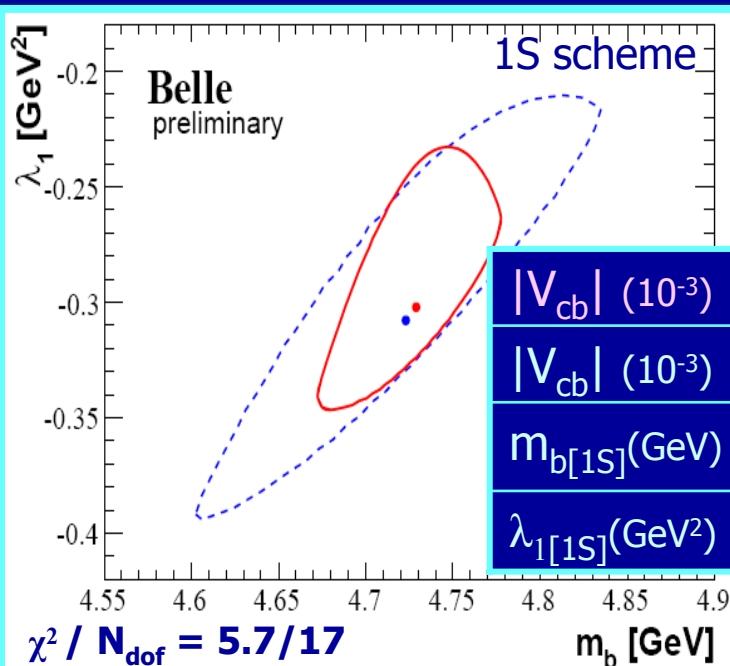
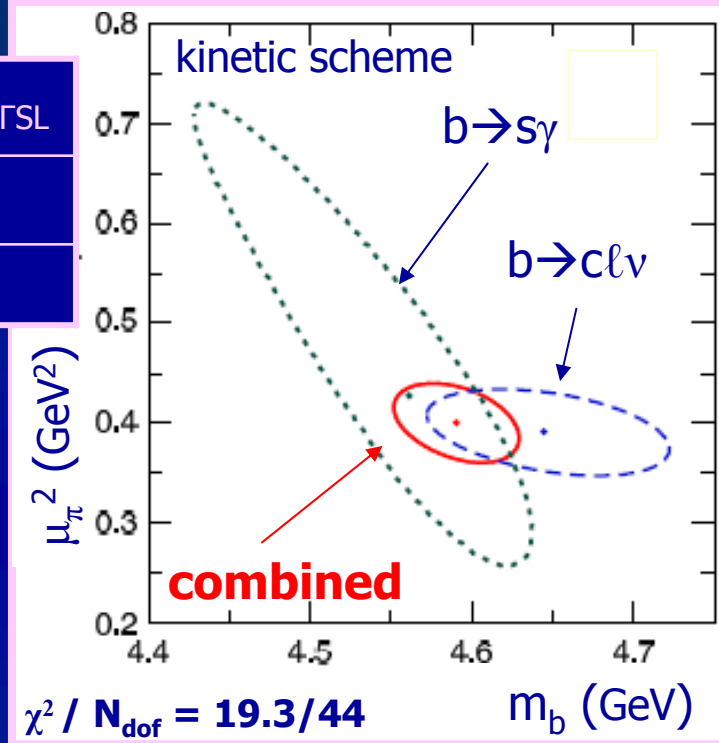
- 47 measured moments used from DELPHI, CLEO, BABAR, BELLE, CDF (and, of course, the B lifetime)

Global fit: results

$|V_{cb}|$ from inclusive decays

$ V_{cb} (10^{-3})$	$41.96 \pm 0.23_{\text{exp}} \pm 0.35_{\text{HQE}} \pm 0.59_{\text{FSL}}$
$m_b [\text{kin}] (\text{GeV})$	$4.59 \pm 0.025_{\text{exp}} \pm 0.030_{\text{HQE}}$
$\mu_\pi^2 [\text{kin}] (\text{GeV}^2)$	$0.401 \pm 0.019_{\text{exp}} \pm 0.035_{\text{HQE}}$

$|V_{cb}|$ determined to $<2\%$
 Only $\sin\theta_c$ known better!



New!

$ V_{cb} (10^{-3})$	$42.0 \pm 0.7_{\text{fit}} \pm 0.5_{\alpha_s} \pm 0.6_{\text{th}}$
$ V_{cb} (10^{-3})$	$41.5 \pm 0.5_{\text{fit}} \pm 0.2_{\tau_B}$
$m_{b[1S]} (\text{GeV})$	$4.73 \pm 0.05_{\text{fit}}$
$\lambda_{1[1S]} (\text{GeV}^2)$	$-0.30 \pm 0.04_{\text{fit}}$

Buchmüller and Flächer,
 PRD 73: 073008 (2006)

m_b to 1%;
 crucial for $|V_{ub}|$

[kin]/[1S] values agree after
 scheme translation

See talks of Dubitzky,
Schwanda, S10



$$\begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}|e^{-i\gamma} \\ |V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}|e^{-i\beta} & |V_{ts}| & |V_{tb}| \end{pmatrix}$$

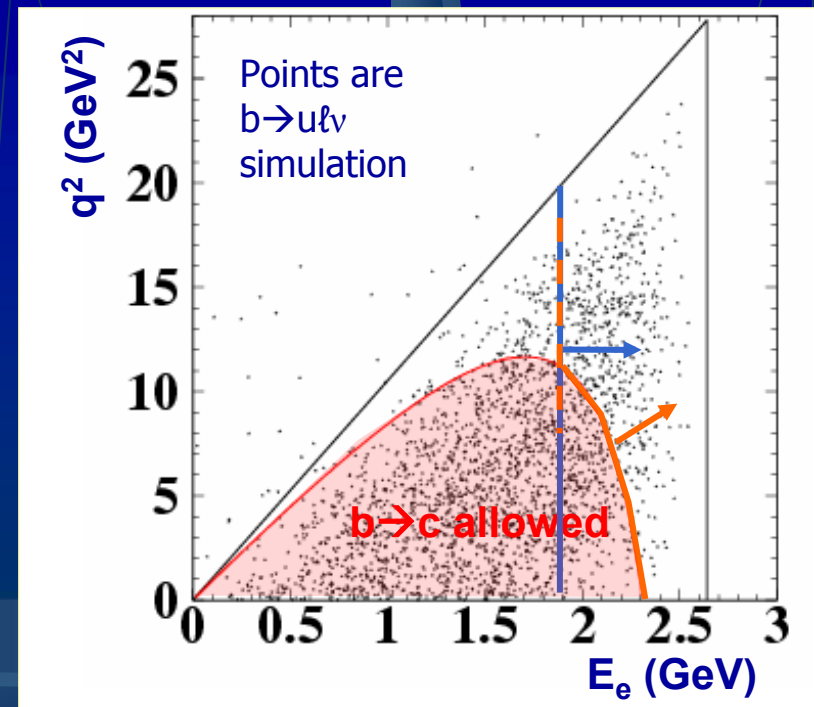
Inclusive $|V_{ub}|$

Strategies for isolating $b \rightarrow u \ell \nu$ decays



- Background $b \rightarrow c \ell \nu$ rate is 50 times signal
- Restrict kinematics to suppress background: challenge for theory
 - OPE convergence is compromised:
 - Need light-cone distribution (shape) function of b quark
 - Relate $b \rightarrow u \ell \nu$ directly to $b \rightarrow s \gamma$ (e.g. Lange, Neubert, Paz, JHEP 0510:084, 2005)
- Measure $b \rightarrow u$ rate in regions dominated by $b \rightarrow c$
 - Theory fine; must fight large uncertainties from background

In all cases sensitivity to m_b^N , $N \gg 5$

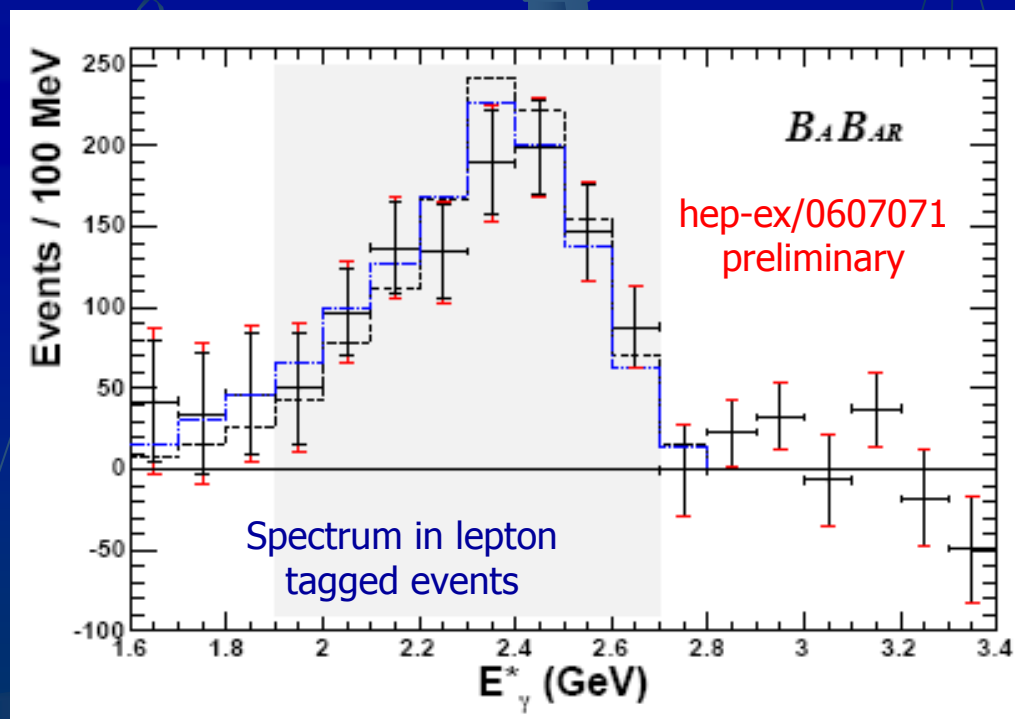


Shape function

- $b \rightarrow s\gamma$ spectrum measured by CLEO, Belle, BaBar
- SF moments related to HQE parameters

$$\langle E_\gamma \rangle \approx \frac{m_b}{2}, \quad \langle E_\gamma^2 - \langle E_\gamma \rangle^2 \rangle \propto \mu_\pi^2$$

- Subleading shape functions differ in $b \rightarrow s\gamma$, $b \rightarrow u\ell\nu$



New measurements

BaBar result: PRL 96:221801 (2006)

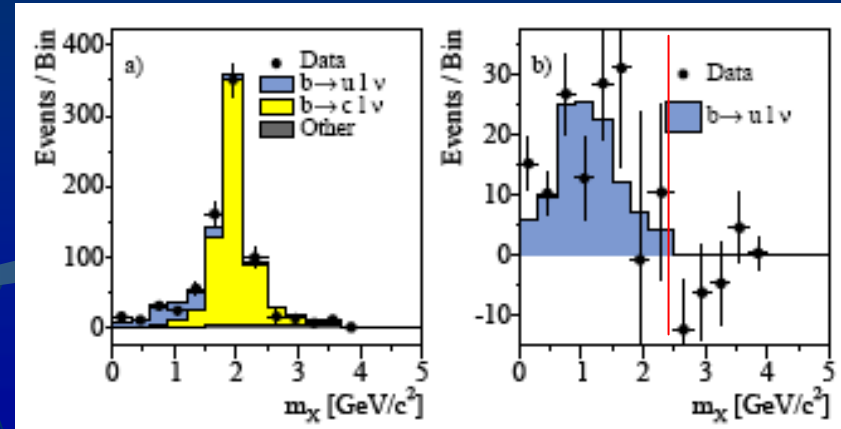
- Fully reconstruct 1 B meson; study semileptonic decay of other B

- Relate $\int_0^{m_{\max}} \frac{d\Gamma_{b \rightarrow u}}{dm_X} dm_X$ to $\int_{E_{\min}}^{m_B/2} \frac{d\Gamma_{b \rightarrow s\gamma}}{dE_\gamma} W(E_\gamma, E_{\min}) dE_\gamma$

$$|V_{ub}| = (4.43 \pm 0.38 \pm 0.25 \pm 0.29) 10^{-3}$$

- Measure up to $m_X < 2.5 \text{ GeV}$

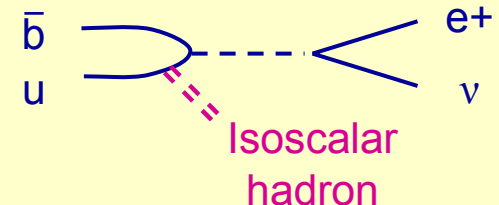
$$|V_{ub}| = (3.84 \pm 0.70 \pm 0.30 \pm 0.10) 10^{-3}$$



Theory errors are small

Will improve – only $88 \times 10^6 \text{ B}\bar{\text{B}}$ used so far

CLEO limit Weak Annihilation contributions:
 $\Gamma_{\text{WA}} / \Gamma_{b \rightarrow u} < 7.4\% \text{ (90\% CL) PRL 96:121801 (2006)}$



Theory calculations



- Two sets of calculations in use for $b \rightarrow s\gamma$ and $b \rightarrow u\ell\nu$
 - Bosch, Lange, Neubert, Paz (BLNP): 3-scale OPE based on HQET, SCET
 - Andersen, Gardi (DGE): parton-level calculation, only m_b and Λ_{QCD} input
- Both provide good description of data; give similar results
- Bauer, Ligeti, Luke (BLL): $|V_{ub}|$ using m_X - q^2 cuts

PRD 72:073006 (2005)

JHEP 0601:097 (2006)

PRD 64:113004 (2001)

Determination of $|V_{ub}|$

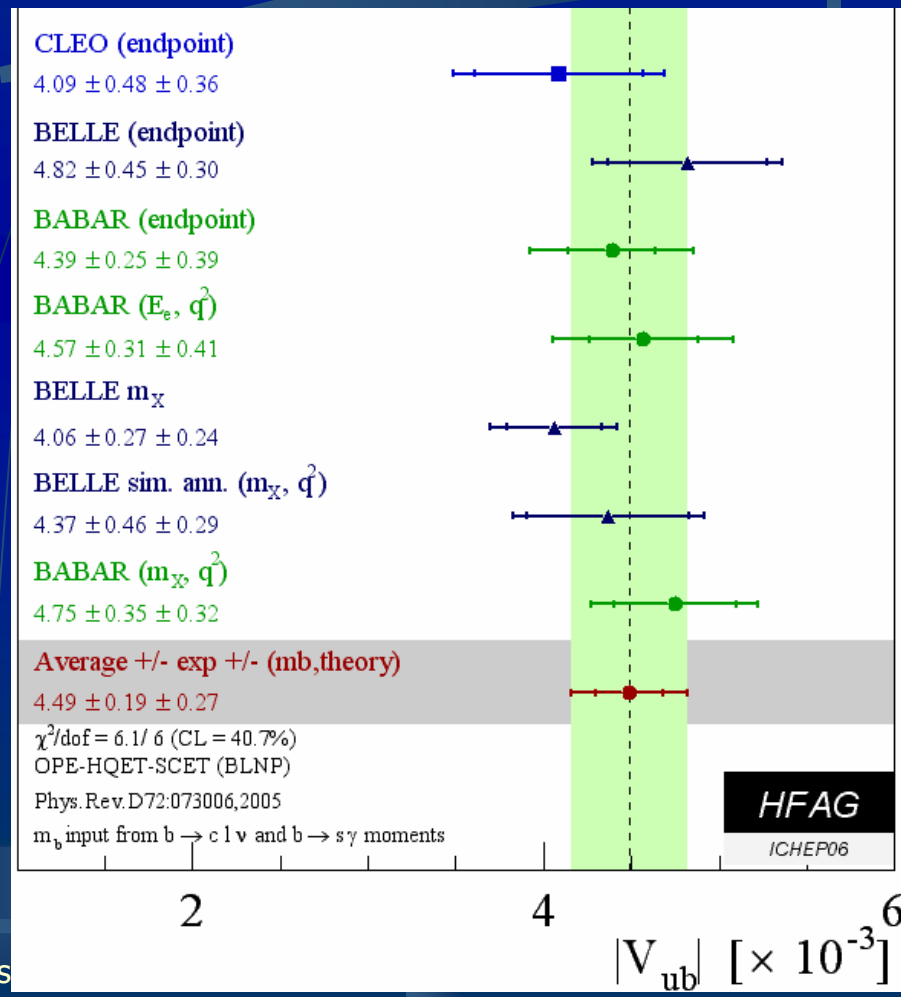


$$|V_{ub}| = (4.49 \pm 0.19 \pm 0.27) \times 10^{-3} \text{ (BLNP)}$$

Major progress since last ICHEP

- Good C.L. = 41%
- Error budget (in %; total 7.3) :

$\pm 2.2_{\text{stat}}$	$\pm 2.8_{\text{exp}}$	$\pm 1.9_{\text{WA}}$	} $\sim \text{exp}$
$\pm 1.9_{\text{b2c model}}$	$\pm 1.6_{\text{b2u model}}$		
$\pm 4.2_{\text{HQ param}}$	$\pm 3.8_{\text{sub SF}}$		} $\sim \text{theory}$
- DGE: $(4.46 \pm 0.20 \pm 0.20) \times 10^{-3}$
C.L. = 12%
- BLL m_X - q^2 : $(5.02 \pm 0.26 \pm 0.37) \times 10^{-3}$
C.L. = 77%
- Many measurements use small fraction of current data samples.
Aggressive target for 2008 is 5%



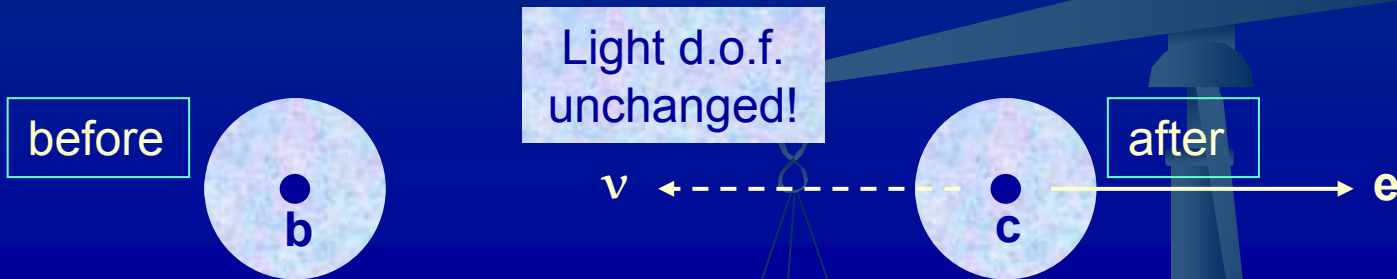


$$\begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}|e^{-i\gamma} \\ |V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}|e^{-i\beta} & |V_{ts}| & |V_{tb}| \end{pmatrix}$$

Exclusive $|V_{cb}|$

Exclusive $b \rightarrow c \ell \nu$ decays

- Heavy-to-heavy transition; HQ symmetry applies $\rightarrow$ unique, universal FF, unit normalization at zero recoil



$$\frac{d\Gamma(B \rightarrow D^* \ell \nu)}{dw} = \frac{G_F^2 |V_{cb}|^2}{48\pi^3} \underbrace{F(w)}_{\text{form factors}} \underbrace{G(w)}_{\text{phase space}}$$

D^* boost in the B rest frame

$$w \equiv \frac{m_B^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}}; \quad 1 < w < 1.504$$

$B \rightarrow D^* \ell \bar{\nu}$ form factor

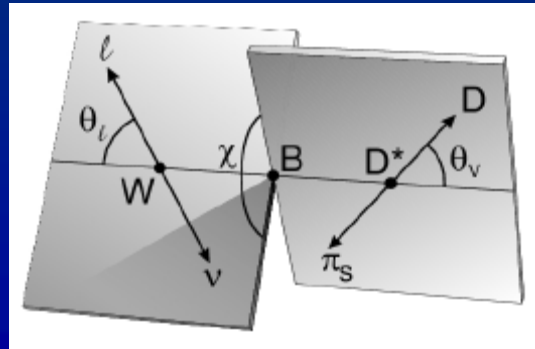
- 3 non-trivial form factors; 4 observables:
 w and 3 angles

HQET-params:

$$\rho^2 = -d\mathbf{F}/dw \big|_{w=1}$$

$$R_1 \sim V/A_1 \text{ and}$$

$$R_2 \sim A_2/A_1$$



- Two measurements from BaBar; averaged values:

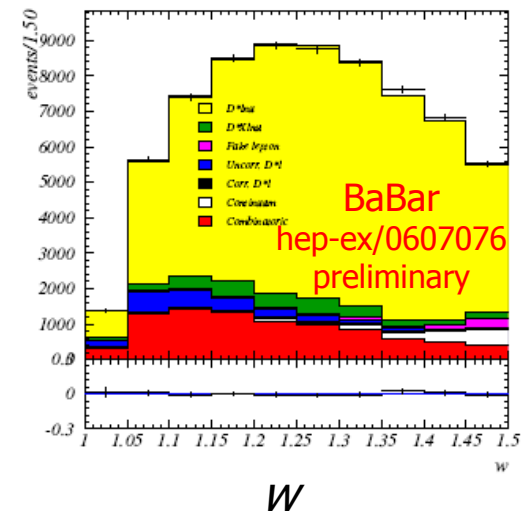
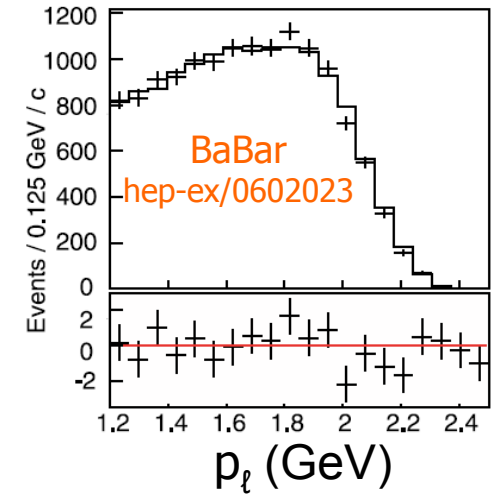
$$\rho^2 = 1.179 \pm 0.048 \pm 0.028$$

$$R_1 = 1.417 \pm 0.061 \pm 0.044$$

$$R_2 = 0.836 \pm 0.037 \pm 0.022$$

$$\mathbf{F}(1)|V_{cb}| = (34.68 \pm 0.32 \pm 1.15) \times 10^{-3}$$

$$\text{BF}(B^0 \rightarrow D^{*+} \ell^- \bar{\nu}) = 4.84 \pm 0.39\%$$



$|V_{cb}|$ from $B \rightarrow D^{(*)} \ell \nu$

- New HFAG average including updated form-factors

$$F(1)|V_{cb}| = (36.2 \pm 0.8) \times 10^{-3}$$

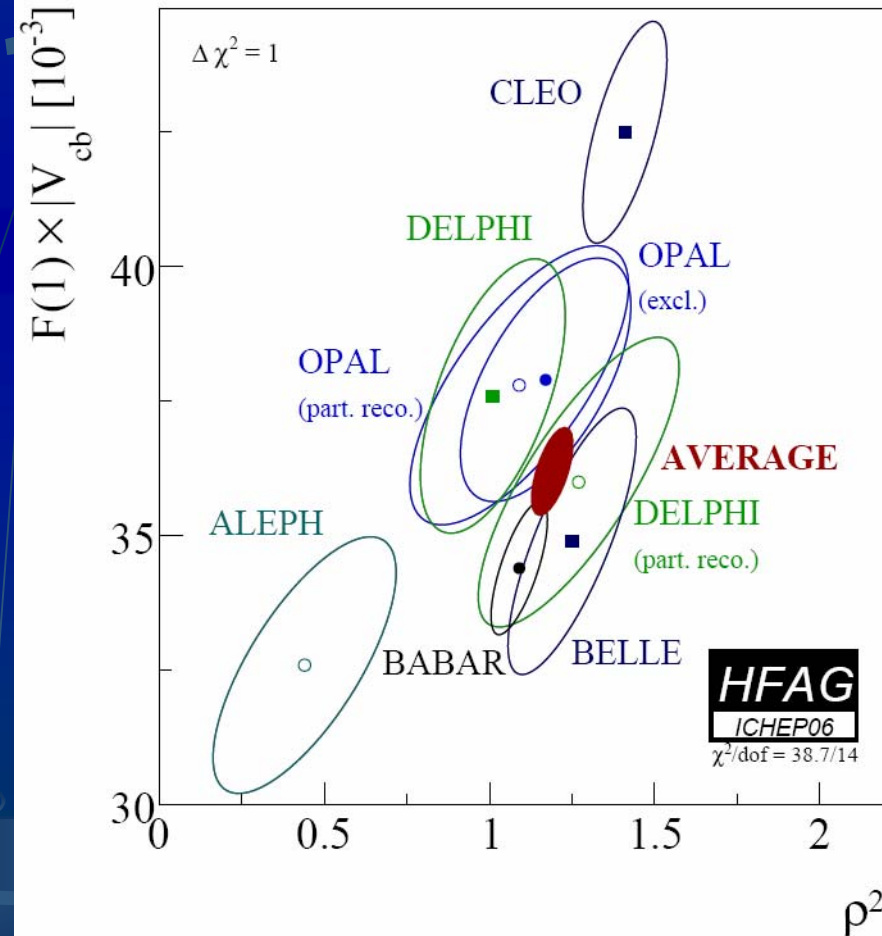
- Using $F(1) = 0.919^{+0.030}_{-0.035}$

(Quenched LQCD, PRD 66:014503 (2002))

$$|V_{cb}| = (39.4 \pm 0.87^{+1.56}_{-1.24}) \times 10^{-3}$$

(inclusive: $|V_{cb}| = (42.0 \pm 0.7) \times 10^{-3}$)

- Work needed on both experiment and theory to reach the precision of the inclusive determination
- Similar measurements on $B \rightarrow D \ell \bar{\nu}$ are harder; in progress



See talks of Dubitzky,
Schwanda, S10

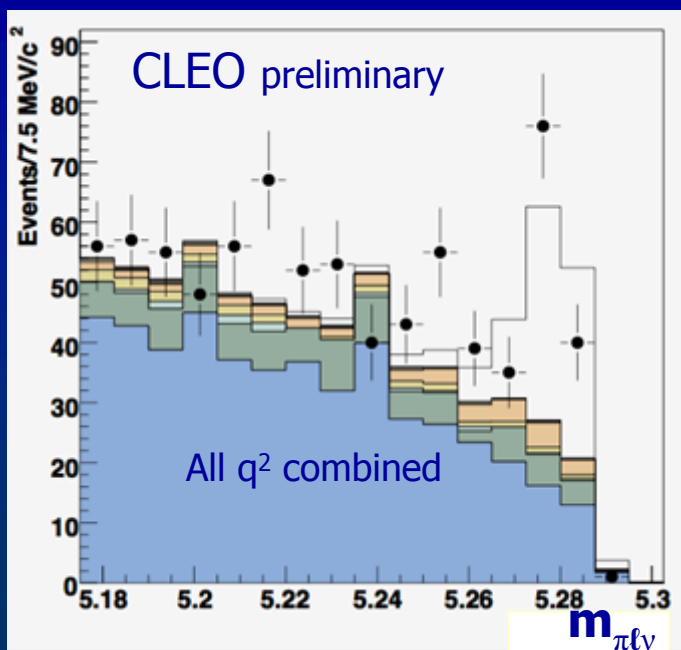


$$\begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}|e^{-i\gamma} \\ |V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}|e^{-i\beta} & |V_{ts}| & |V_{tb}| \end{pmatrix}$$

Exclusive $|V_{ub}|$

$B \rightarrow \pi \ell \nu$

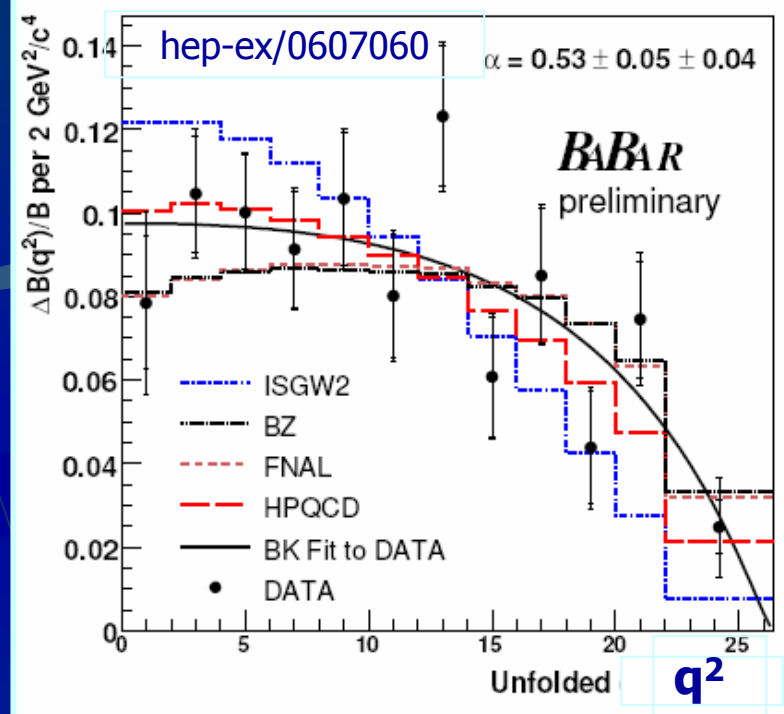
- New BaBar $B^0 \rightarrow \pi^- \ell^+ \nu$
 - High statistics ν -reco method
 - Significantly improved precision
 - ISGW2 model: C.L. = 0.07%
 - Data consistent with Lattice QCD and Becirevic-Kaidalov



$$\text{BF}(B \rightarrow \pi \ell \nu) = (1.44 \pm 0.08 \pm 0.10) \times 10^{-4}$$

$$\Delta \text{BF}(q^2 > 16 \text{ GeV}^2) = (0.37 \pm 0.04 \pm 0.03) \times 10^{-4}$$

$$\alpha_{\text{BK}} = 0.53 \pm 0.05 \pm 0.04$$



- New CLEO $B^0 \rightarrow \pi^-/\rho^- \ell^+ \nu$ preliminary
 - Good quality ν -reco

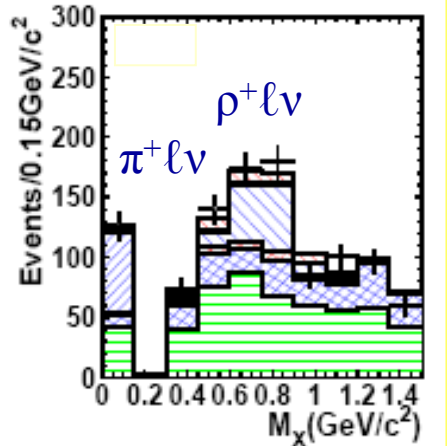
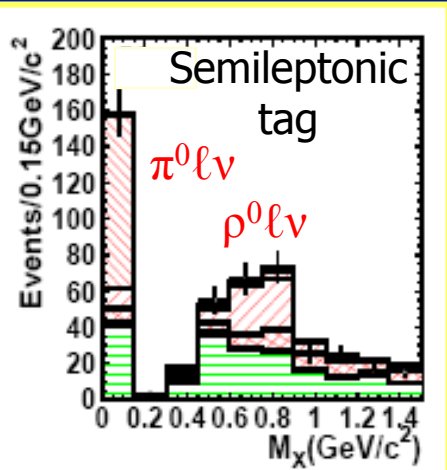
$$\text{BF}(B \rightarrow \pi \ell \nu) = (1.37 \pm 0.16 \pm 0.13) \times 10^{-4}$$

$$\Delta \text{BF}(q^2 > 16 \text{ GeV}^2) = (0.40 \pm 0.08 \pm 0.05) \times 10^{-4}$$

$$\text{BF}(B \rightarrow \rho \ell \nu) = (2.91 \pm 0.38 \pm 0.38) \times 10^{-4}$$

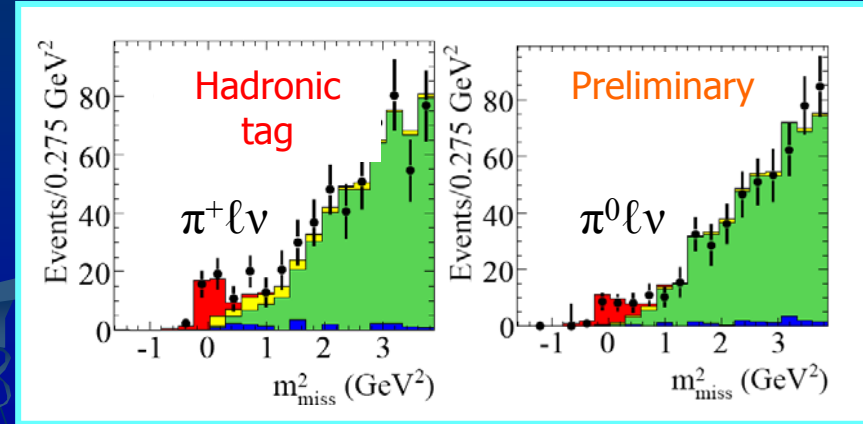
$B \rightarrow \pi \ell \nu$ with low background

- Reconstruct (tag) one B in hadronic or semileptonic decay
- Compare what's left with signal



BaBar $\rightarrow$
211 fb⁻¹

← Belle
253 fb⁻¹



BF (10 ⁻⁴)	Belle hep-ex/0604024	BaBar hep-ex/0607089
$\pi^+ \ell \nu$ (s.l. tag)	$1.38 \pm 0.19 \pm 0.14$	$1.12 \pm 0.25 \pm 0.10$
$\pi^0 \ell \nu$ (s.l. tag) $\times 2\tau_0/\tau_+$	$1.43 \pm 0.26 \pm 0.16$	$1.35 \pm 0.33 \pm 0.19$
$\pi^+ \ell \nu$ (had tag)	$1.49 \pm 0.26 \pm 0.06$	$1.07 \pm 0.27 \pm 0.19$
$\pi^0 \ell \nu$ (had tag) $\times 2\tau_0/\tau_+$	$1.60 \pm 0.32 \pm 0.11$	$1.52 \pm 0.41 \pm 0.20$
$\rho^0 \ell \nu / \eta \ell \nu$	$1.33 \pm 0.23 \pm 0.18$	$0.84 \pm 0.27 \pm 0.21$
$\rho^+ \ell \nu / \eta' \ell \nu$	$2.17 \pm 0.54 \pm 0.32$	< 1.3

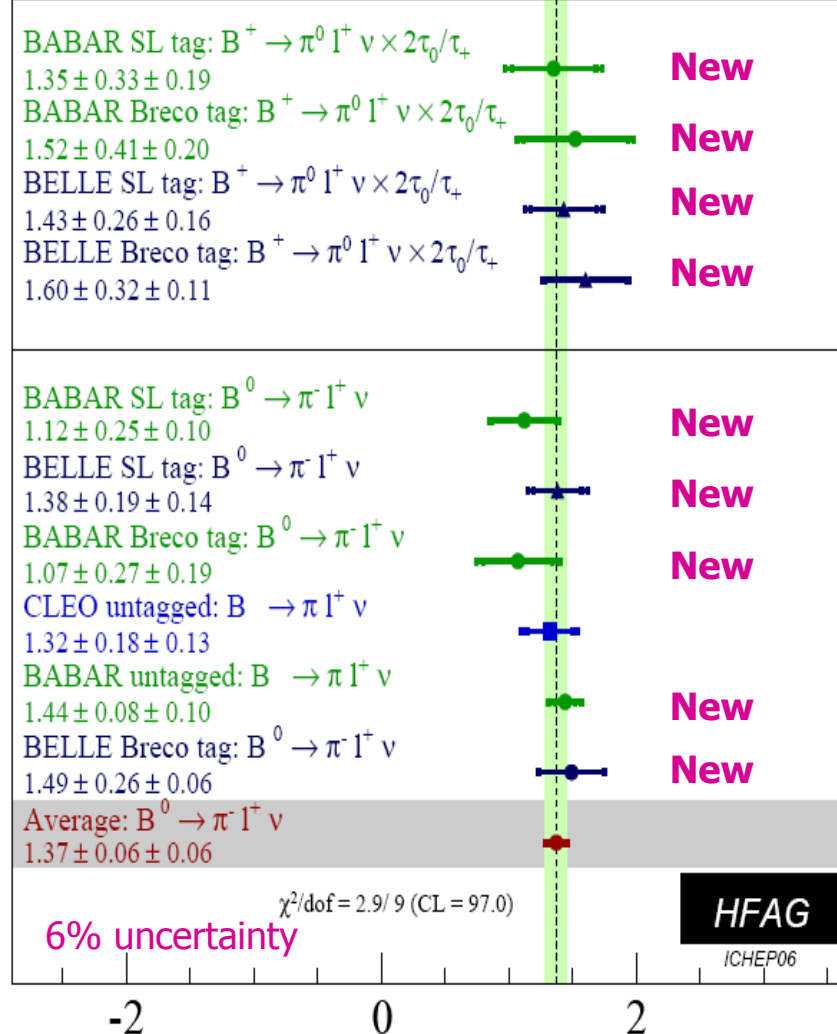
$|V_{ub}|$ from $B \rightarrow \pi \ell \nu$

- Averages of tagged and untagged methods are comparable

For $|V_{ub}|$:

- Lattice QCD: $q^2 > 16 \text{ GeV}^2$
- Light-cone sum rules: $q^2 < 16 \text{ GeV}^2$
- FF normalization errors dominate; task for theory, CLEO-c

(inclusive: $|V_{ub}| = (4.49 \pm 0.34) \times 10^{-3}$)



FF calc	$V_{ub} [10^{-3}]$	FF norm (ps^{-1})	Ref
Ball-Zwicky	$3.38 \pm 0.12^{+0.56}_{-0.37}$	5.44 ± 1.43	PRD 71:014015 (2005)
HPQCD	$3.93 \pm 0.26^{+0.59}_{-0.41}$	1.46 ± 0.35	PRD 73:074502 (2006)
FNAL	$3.51 \pm 0.23^{+0.61}_{-0.40}$	1.83 ± 0.50	hep-lat/0409116
APE	$3.54 \pm 0.23^{+1.36}_{-0.63}$	1.80 ± 0.86	Nucl. Phys. B619:565 (2000)

$B(B^0 \rightarrow \pi^- l^+ \nu) [\times 10^{-4}]$

Experimental
error on $|V_{ub}|$
 $\sim 6\%$

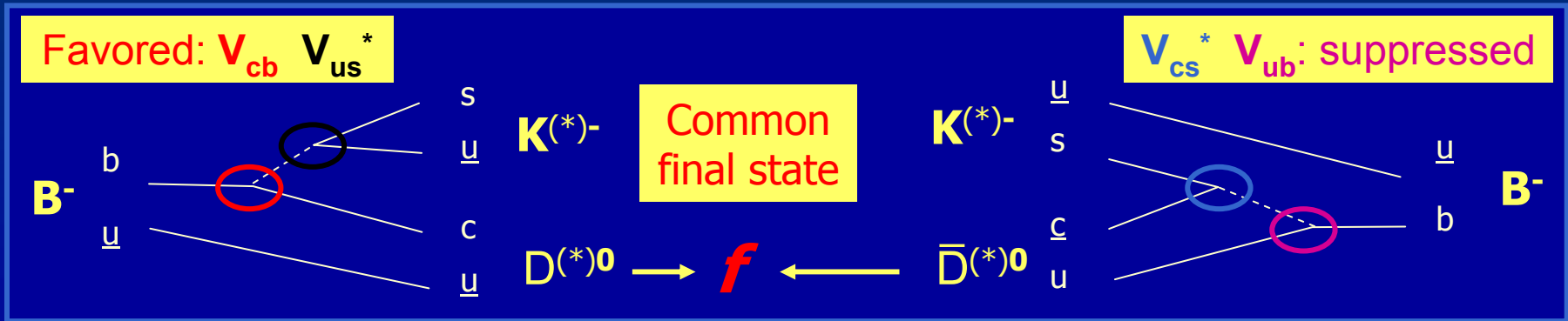


$$\begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}| e^{-i\gamma} \\ |V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}| e^{-i\beta} & |V_{ts}| & |V_{tb}| \end{pmatrix}$$

The phase: γ (Φ_3)

The relative phase γ (φ_3)

Interference between tree-level decays; theoretically clean



$$\frac{A(B^- \rightarrow \bar{D}^0 K^-)}{A(B^- \rightarrow D^0 K^-)} = r_B e^{i\delta_B} e^{-i\gamma}$$

Parameters: γ ,
(r_B , δ_B) per mode

Three methods for exploiting interference (choice of D^0 decay modes):

- Gronau, London, Wyler (GLW): Use CP eigenstates of $D^{(*)0}$ decay, e.g. $D^0 \rightarrow K_S \pi^0$, $D^0 \rightarrow \pi^+ \pi^-$
- Atwood, Dunietz, Soni (ADS): Use doubly Cabibbo-suppressed decays, e.g. $D^0 \rightarrow K^+ \pi^-$
- Giri, Grossman, Soffer, Zupan (GGSZ) / Belle: Use Dalitz plot analysis of 3-body D^0 decays, e.g. $K_S \pi^+ \pi^-$

GLW-based analyses

- Measure asymmetry between B^+/B^- for CP even/odd D decays

$$\mathcal{A}_{CP\pm} = \frac{\Gamma(B^- \rightarrow D_{\pm} K^-) - \Gamma(B^+ \rightarrow D_{\pm} K^+)}{\Gamma(B^- \rightarrow D_{\pm} K^-) + \Gamma(B^+ \rightarrow D_{\pm} K^+)} = \frac{\pm 2r_B \sin \delta_B \sin \gamma}{1 + r_B^2 \pm 2r_B \cos \delta_B \cos \gamma}$$

8-fold ambiguity on γ

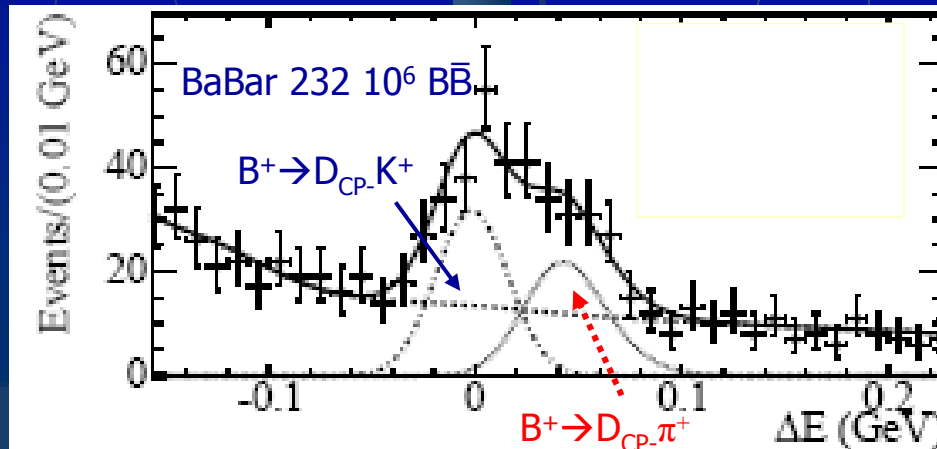
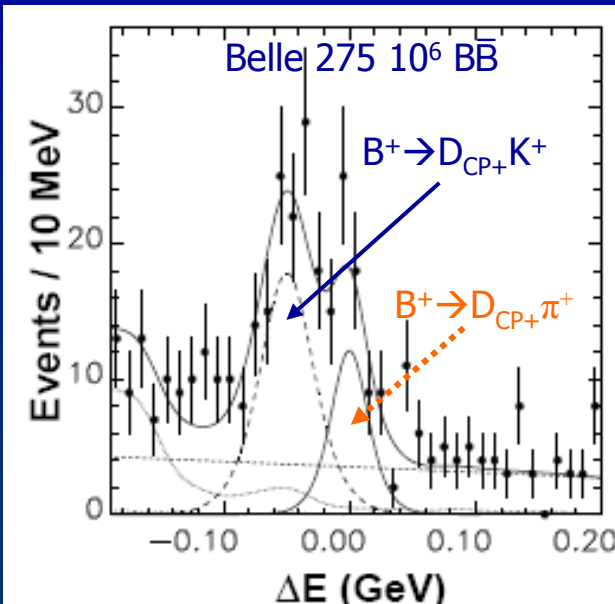
and the fractional decay rates to CP eigenstates:

$$\mathcal{R}_{CP\pm} = \frac{\Gamma(B^- \rightarrow D_{\pm} K^-) + \Gamma(B^+ \rightarrow D_{\pm} K^+)}{\Gamma(B^- \rightarrow D^0 K^-) + \Gamma(B^+ \rightarrow \bar{D}^0 K^+)} = 1 + r_B^2 \pm 2r_B \cos \delta_B \cos \gamma$$

Hard to disentangle r_B
from γ and δ_B

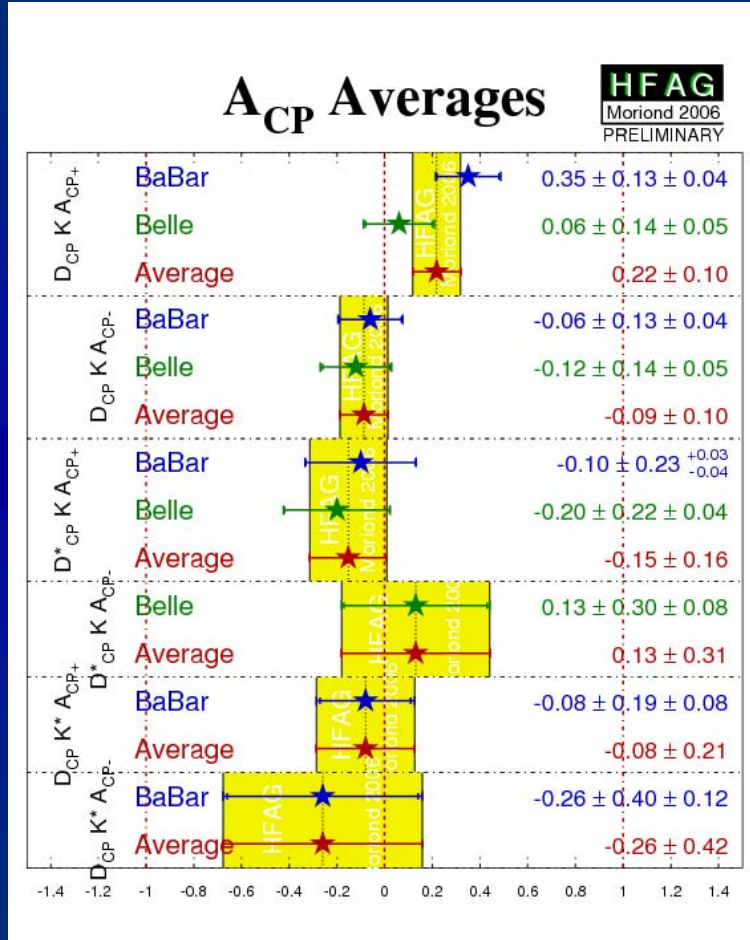
Recent results: Belle (PRD 73:051106, 2006), BaBar (PRD 73: 051105, 2006)

Signals seen in CP-even and CP-odd D decays

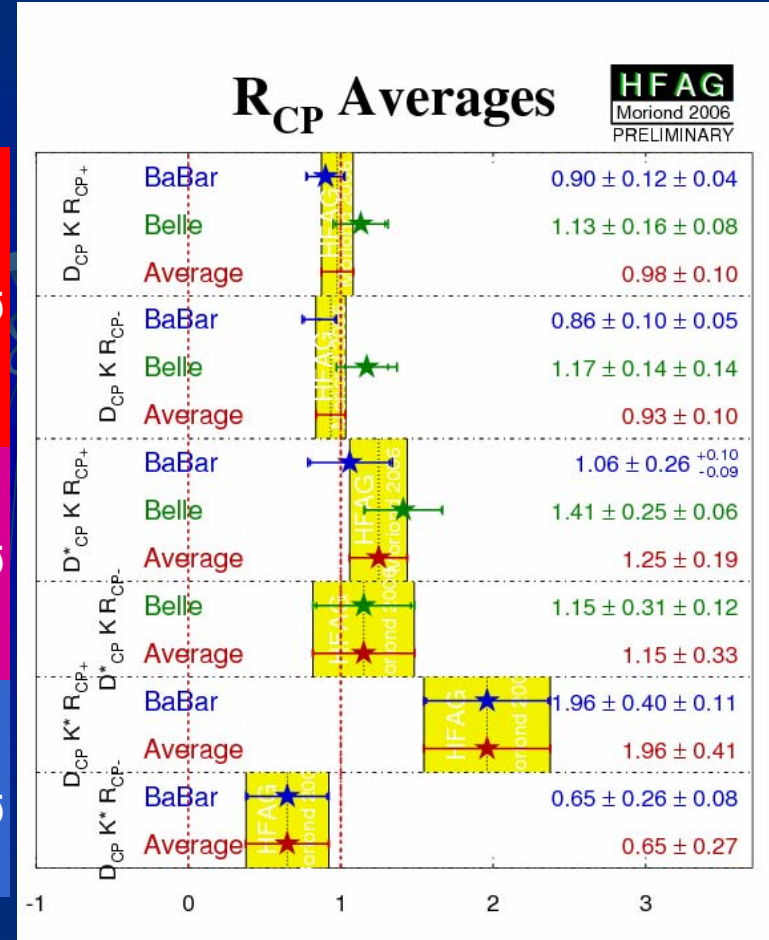


Similar measurements exist in $B^+ \rightarrow D^{*0} K^+$

GLW averages



$D_{CP} K$
 $D_{CP}^* K$
 $D_{CP} K^*$



Implications for r_B and γ discussed later

ADS-based analyses

- Use DCS decays to reach same final state, e.g.

avored	suppressed
$B^- \rightarrow D^0 K^- \oplus D^0 \rightarrow K^+ (n \pi)$	
$B^- \rightarrow \bar{D}^0 K^- \oplus \bar{D}^0 \rightarrow K^+ (n \pi)$	
suppressed	avored

Small product BF but
comparable amplitudes $\rightarrow$
large potential asymmetry

Additional
parameters
 r_D and δ_D

$$\frac{A(B^- \rightarrow \bar{D}^0 [K^+ \pi^-] K^-)}{A(B^- \rightarrow D^0 [K^+ \pi^-] K^-)} = r_B e^{i\delta_B} e^{-i\gamma} + r_D e^{-i\delta_D}$$

$$\mathcal{A}_{ADS} = \frac{\Gamma(B^- \rightarrow [K^+ \pi^-] K^-) - \Gamma(B^+ \rightarrow [K^- \pi^+] K^+)}{\Gamma(B^- \rightarrow [K^+ \pi^-] K^-) + \Gamma(B^+ \rightarrow [K^- \pi^+] K^+)} = \frac{2r_B r_D \sin(\delta_B + \delta_D) \sin \gamma}{\mathcal{R}_{ADS}}$$

$$\mathcal{R}_{ADS} = \frac{\Gamma(B^- \rightarrow [K^+ \pi^-] K^-) + \Gamma(B^+ \rightarrow [K^- \pi^+] K^+)}{\Gamma(B^- \rightarrow [K^- \pi^+] K^-) + \Gamma(B^+ \rightarrow [K^+ \pi^-] K^+)} = r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos \gamma$$

Modes $D^* K$ and $D K^*$ also used

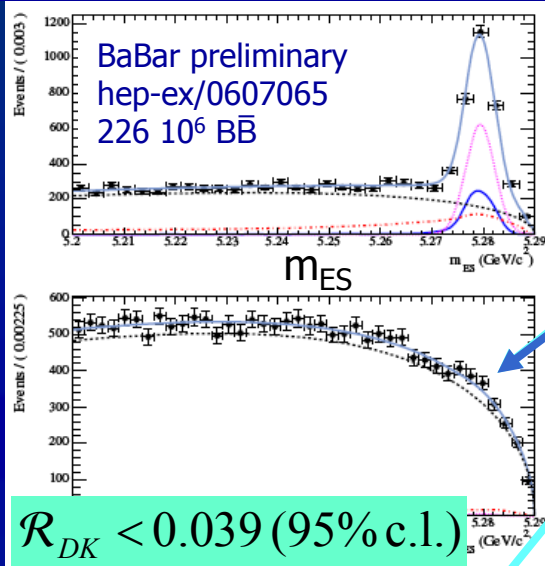
$D^{*0} \rightarrow D^0 \pi$ and $D^{*0} \rightarrow D^0 \gamma$ have opposite CP

Direct
dependence

DCSD charm;
 $r_D(K\pi) = 0.0603 \pm 0.0025$

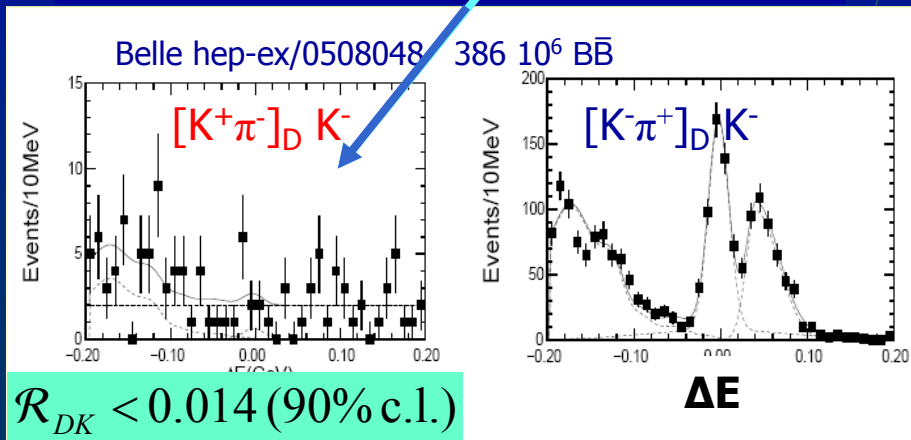
ADS results

New BaBar result in $[K^+\pi\pi^0]_D K^-$



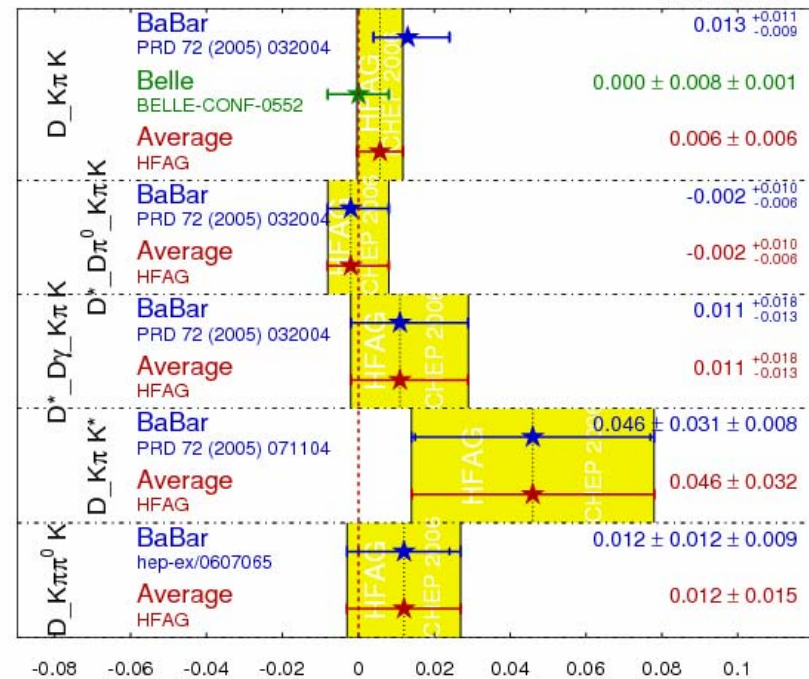
No signal yet in suppressed modes

Belle result in $[K^+\pi^-]_D K^-$



R_{ADS} Averages

HFAG
ICHEP 2006
PRELIMINARY



Implications for r_B and γ discussed later

Dalitz analyses



- Measure B^+/B^- asymmetry across Dalitz plot

decay

$$B^\pm \rightarrow [K_s \pi^+ \pi^-]_D K^\pm$$

amplitude

$$A_\pm = f(m_+^2, m_-^2) + r_B e^{\pm i\gamma} e^{i\delta_B} f(m_-^2, m_+^2)$$

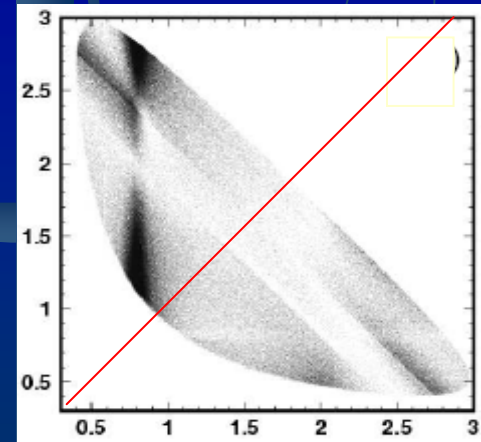
$$m_\pm^2 \Rightarrow m^2(K_s \pi^\pm)$$

Sensitivity to γ in interference term

Determine f in flavor-tagged $D^{*+} \rightarrow D^0 \pi^+$ decays

- Includes GLW ($D^0 \rightarrow K_s \rho^0$, CP eigenstate) and ADS ($D^0 \rightarrow K^{*+} \pi^-$, DCS 2-body decay) regions

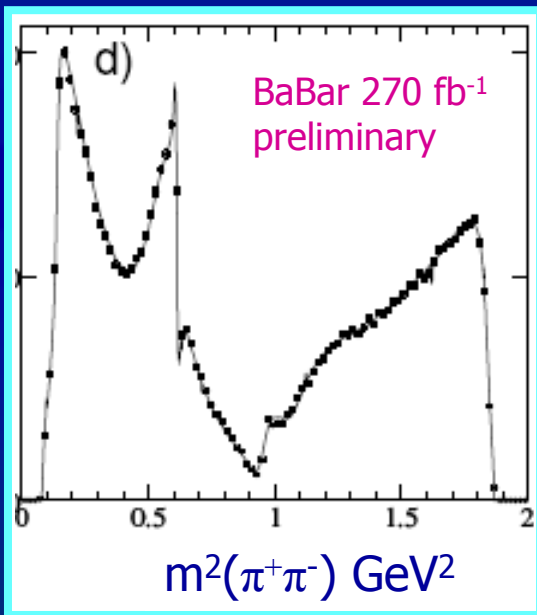
Mirror symmetry
between D^0 and $\bar{D}^0$
Dalitz plots



2-fold ambiguity on γ : $(\gamma, \delta) \rightarrow (\gamma + \pi, \delta + \pi)$

Dalitz model for $K_S \pi^+ \pi^-$

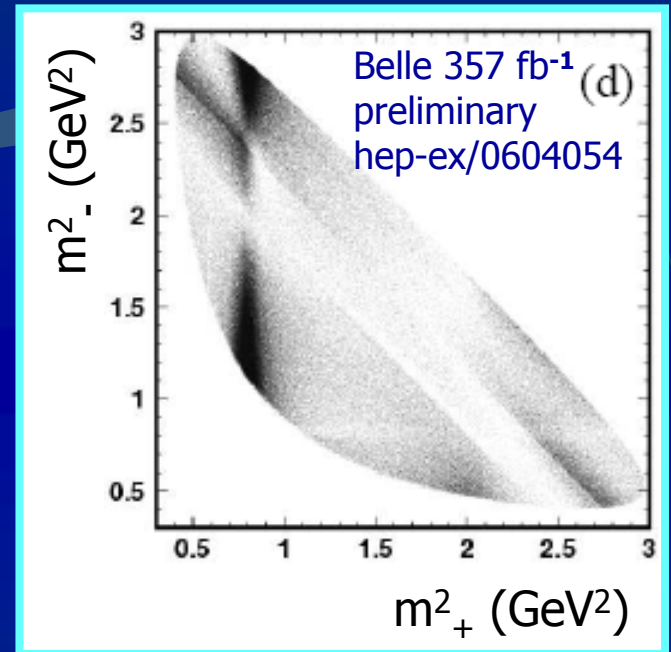
- Select $D^{*+} \rightarrow [K_S \pi^+ \pi^-] \pi^+$ from $e^+ e^- \rightarrow c \bar{c}$; $\sim 4 \cdot 10^5$ events
- Fit to coherent sum of 15-16 Breit-Wigner amplitudes plus a non-resonant term



Excellent fits obtained

Main contributors:

- $K^{*-}(892) \pi^+$
- $K_S \rho^0$
- $K^{*0}(1430) \pi^-$
- $K^{*-}(892) \pi^+$
- non/broad resonant

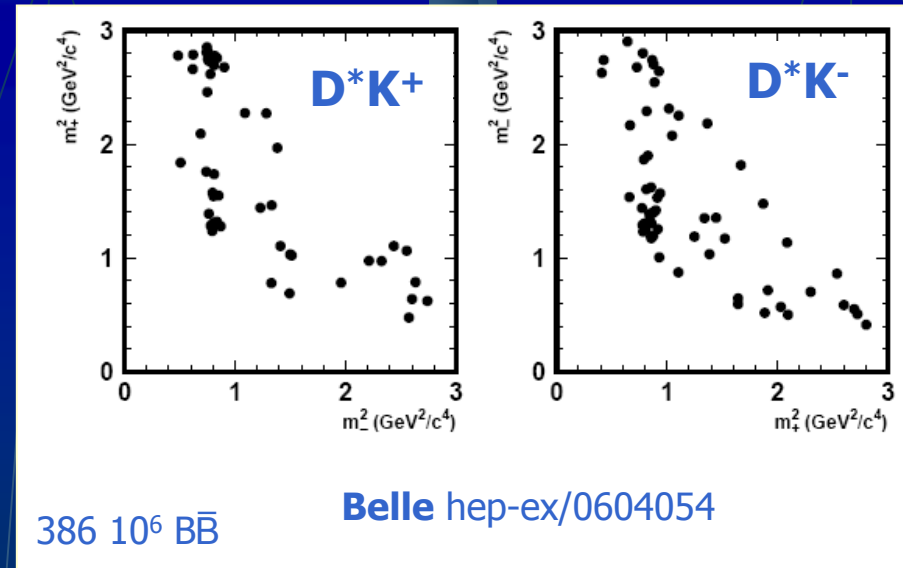
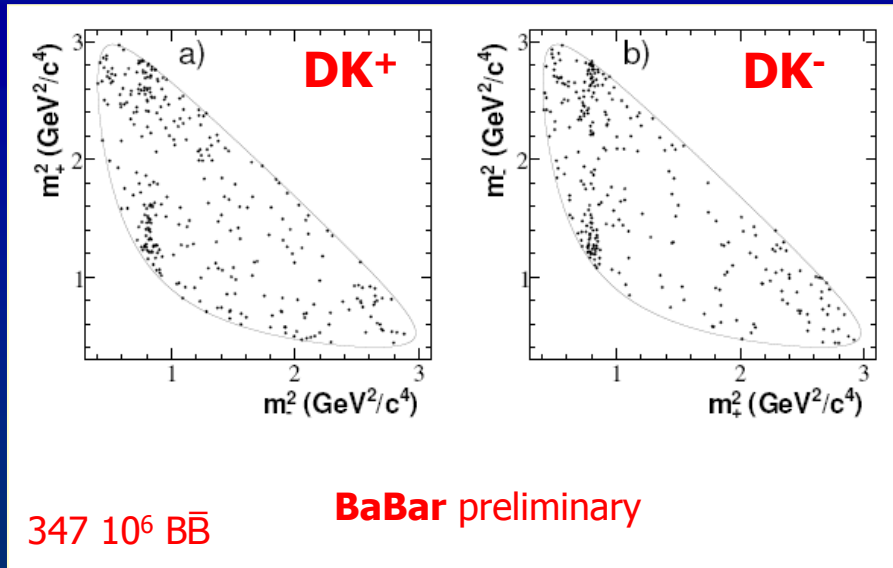


Improved modeling (e.g. K-matrix formulation) under study

Model-independent approach (GGSZ) using CP-tagged D^0 studied by Bondar, Poluektov in hep-ph/0510246

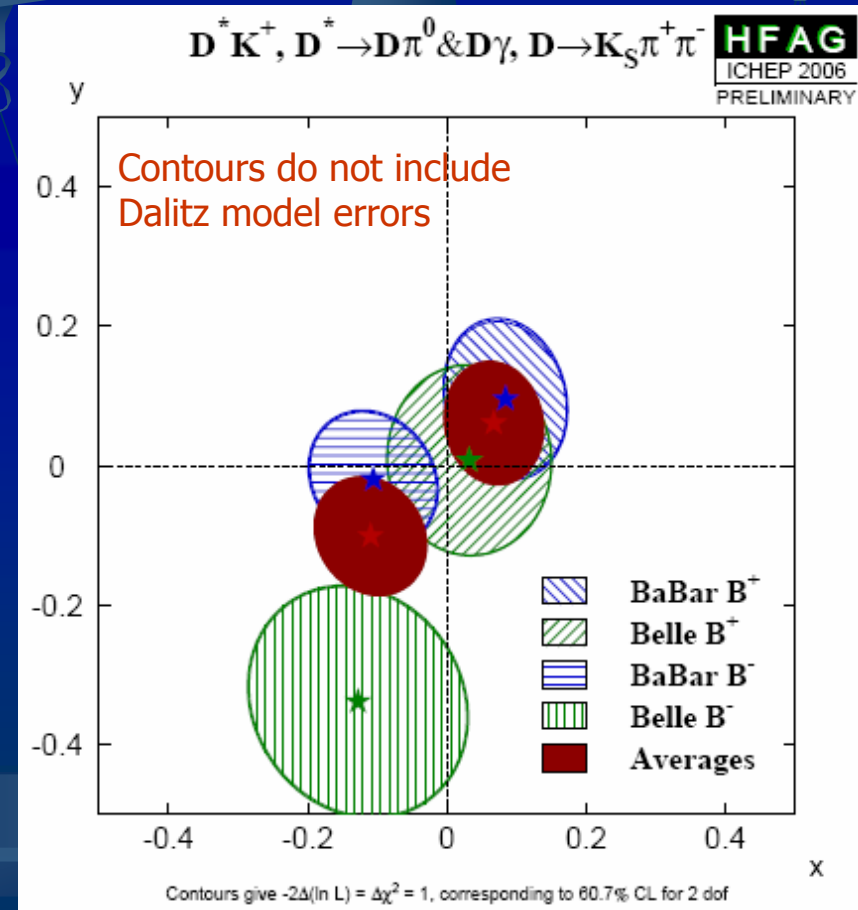
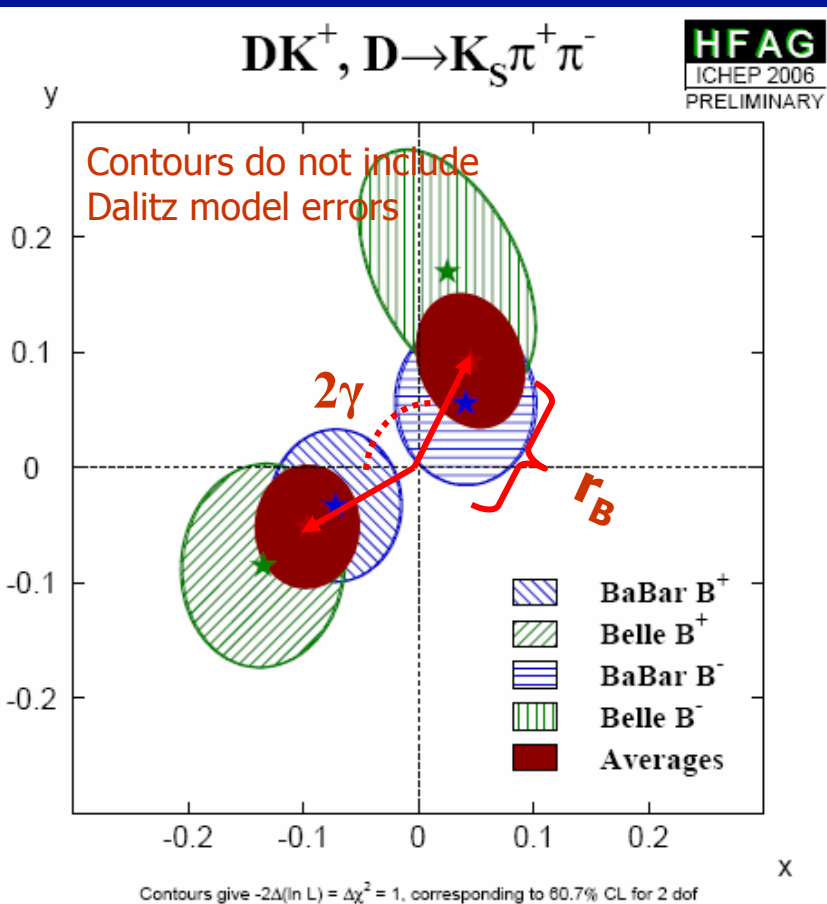
Dalitz plots

- Plots shown are representative; both experiments have analyzed DK, D*K and DK* decays



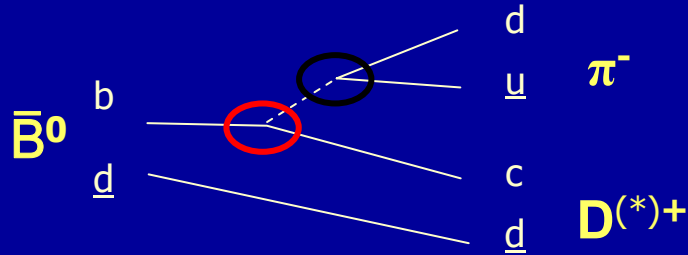
Results on γ

- HFAG averages for $x_{\pm} = r_B \cos(\delta_B \pm \gamma)$, $y_{\pm} = r_B \sin(\delta_B \pm \gamma)$
- UTfit find $\gamma = 78 \pm 30^\circ$ based on $B^- \rightarrow D^{(*)} K^{(*)-}$ decays
- Note: σ_γ depends significantly on the value of r_B

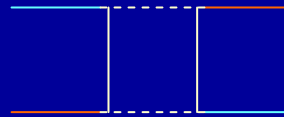


$\sin(2\beta + \gamma)$

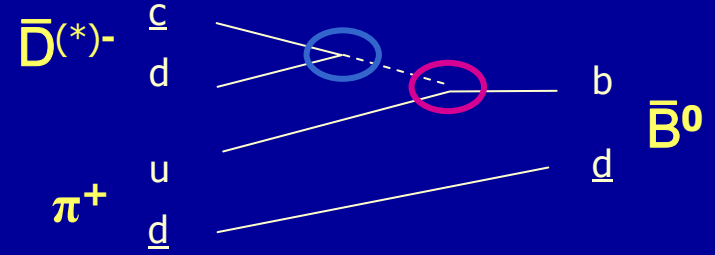
really favored: $V_{cb} V_{ud}^*$



2 common
final states via
 $B\bar{B}$ mixing



$V_{cd}^* V_{ub}$: really suppressed

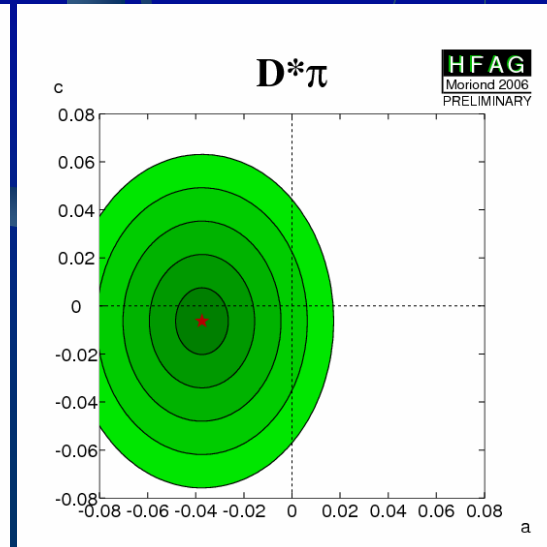
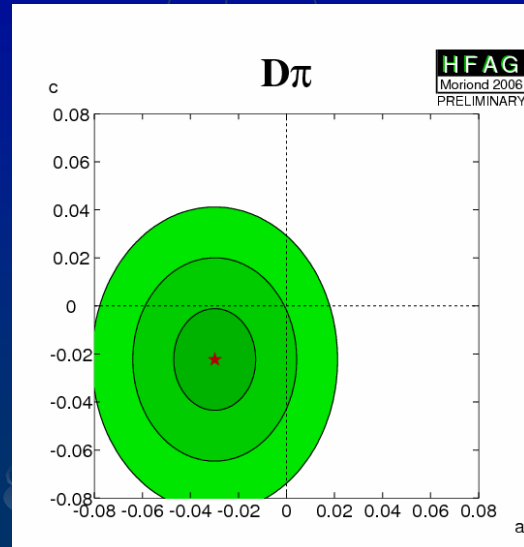


$$\frac{A_{\text{suppressed}}}{A_{\text{favored}}} = r_B e^{i\delta_B} e^{-i(2\beta + \gamma)}$$

Time-dependent effect
(due to $B^0 - \bar{B}^0$ mixing)

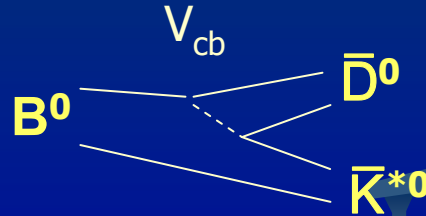
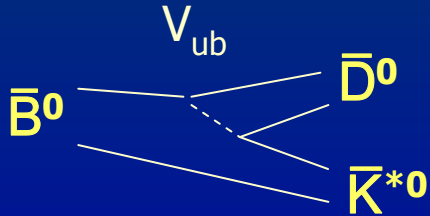
Parameters: $\gamma, 2\beta$
(r, δ_B) per mode

Large BF but small r_B (<2%)
 $\rightarrow$ small CP asymmetry
 r_B must be estimated from
 $B^0 \rightarrow D_s^+ \pi^-$ using SU(3)

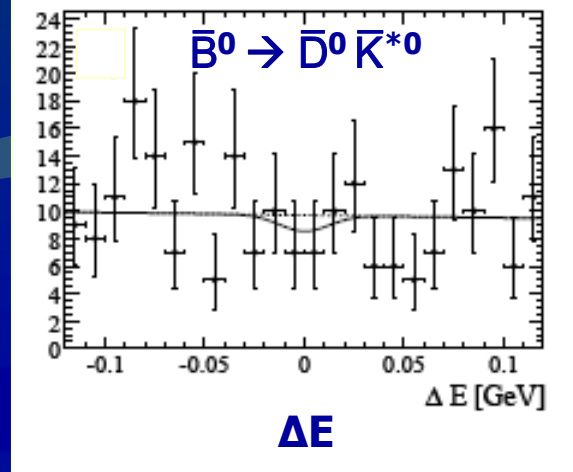


$B^0 \rightarrow D^0 K^0$ feasibility study

The angle $\gamma (\varphi_3)$



BaBar hep-ex/0604016, soon in PRD



- Interference of $\bar{B}^0 \rightarrow \bar{D}^0 \bar{K}^0$ with $\bar{B}^0 \rightarrow B^0 \rightarrow \bar{D}^0 K^0$ (K^0 and $\bar{K}^0$ mix)
- Determine r_{DK^*} in related decay $\bar{B}^0 \rightarrow \bar{D}^0 \bar{K}^{*0}$
- BaBar find no signal: $r_{DK^*} < 0.4$ @90% c.l.
- This mode may be harder to use for $\sin(2\beta+\gamma)$ than predicted; implications for LHC-b

Related measurements



Nice ideas, nice work, but
not much impact yet for γ

$r_{D\pi}$ from $B^0 \rightarrow D_s^{(*)}\pi^-$, SU(3)

BaBar hep-ex/0604012, 226 10^6 BB

$$\left. \begin{aligned} BF(B \rightarrow D_s^+ \pi^-) &= 1.3 \pm 0.3 \pm 0.2 \\ BF(B \rightarrow D_s^{*+} \pi^-) &= 2.8 \pm 0.6 \pm 0.5 \\ BF(B \rightarrow D_s^+ K^-) &= 2.5 \pm 0.4 \pm 0.4 \\ BF(B \rightarrow D_s^{*+} K^-) &= 2.0 \pm 0.5 \pm 0.4 \end{aligned} \right\} \times 10^{-5}$$

$$\Rightarrow \left. \begin{aligned} r_{D\pi} &= 1.3 \pm 0.2 \pm 0.1 \\ r_{D^*\pi} &= 1.9 \pm 0.2 \pm 0.2 \end{aligned} \right\} \times 10^{-2} \quad \text{preliminary}$$

$B^0 \rightarrow \bar{D}^0 K^+ \pi^-$

BaBar PRL 96:011803 (2006)

BaBar show that $B \rightarrow \bar{D}^0 K^+ \pi^-$
not promising for measuring γ

$B^0 \rightarrow D_s a_{0,2}$

BaBar PRD D73 \:071103 (2006)

$$\left. \begin{aligned} BF(B \rightarrow D_s^+ a_0^-) &< 1.9 \\ BF(B \rightarrow D_s^{*+} a_0^-) &< 3.6 \\ BF(B \rightarrow D_s^+ a_2^-) &< 19 \\ BF(B \rightarrow D_s^{*+} a_2^-) &< 20 \end{aligned} \right\} \times 10^{-5}, 90\% \text{ c.l.} \quad 226 \text{ } 10^6 \text{ BB}$$

$B \rightarrow D^* D^*$

BaBar PRD 73:112004 (2006)

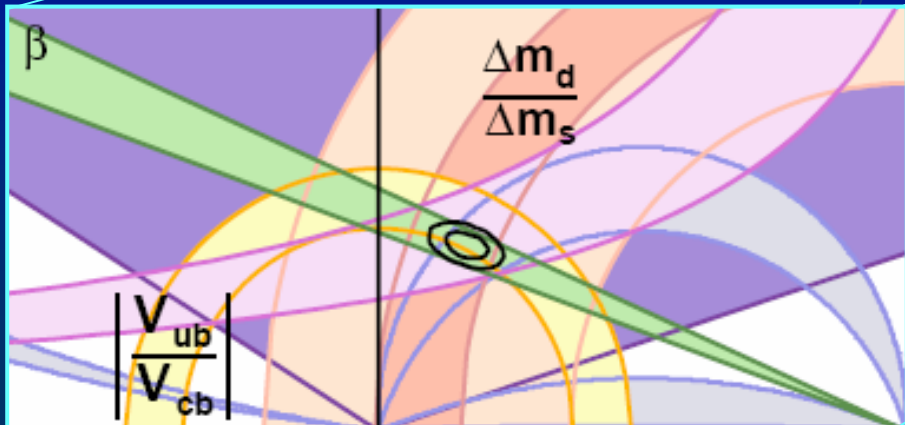
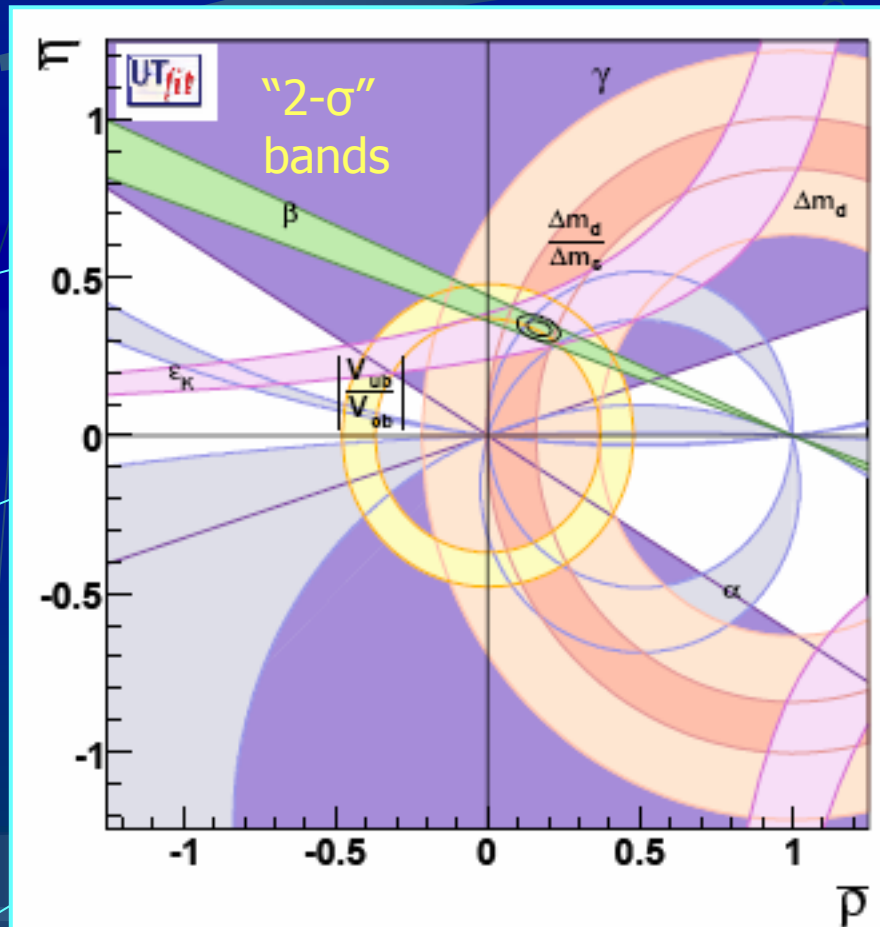
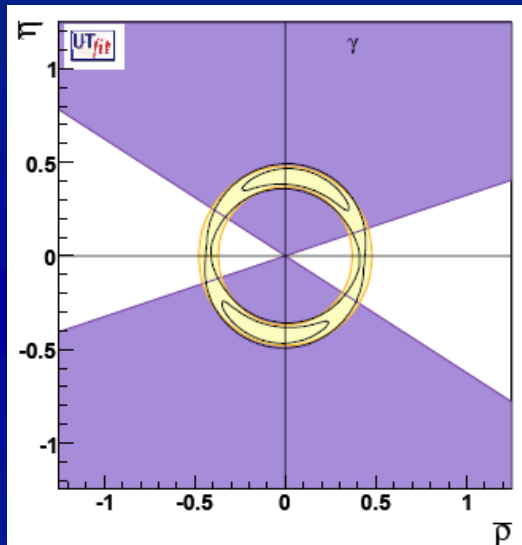
BF and charge asymmetries
measured for all $B \rightarrow D^{(*)}D^{(*)}$
modes; provides input for
 $\sin(2\beta+\gamma)$ from $B^0 \rightarrow D^{(*)}+D^{(*)-}$
time-dependent asymmetries

See talks of Vagnoni, T'Jampens, S8

Current status of UT

Tree-level determination: information on phase γ (φ_3) not yet constraining

All constraints: compatible with SM, but tension exists between $\sin 2\beta$ and $|V_{ub}/V_{cb}|$



The angle γ (φ_3)

Summary

■ Today:

$$|V_{cb}| = (42.0 \pm 0.23 \pm 0.69) \times 10^{-3}$$

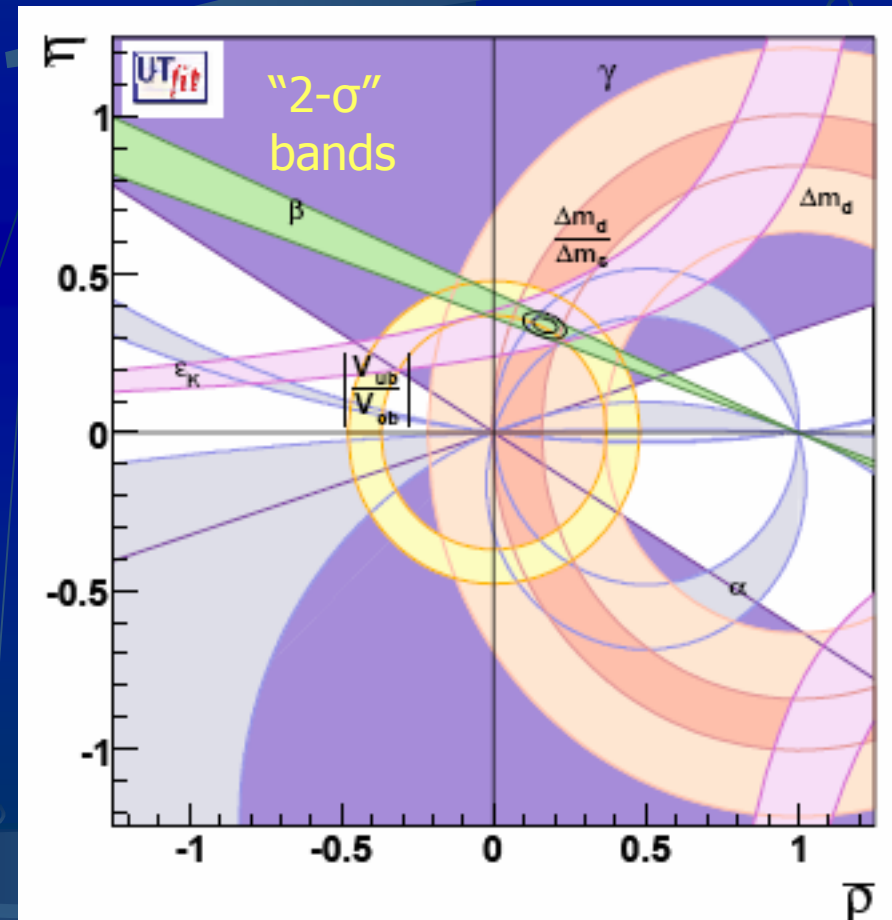
$$|V_{ub}| = (4.49 \pm 0.19 \pm 0.27) \times 10^{-3}$$

$$\gamma(\phi_3) = 78 \pm 30^\circ$$

■ What to look for in 2008:

- 2 ab^{-1} from the B factories (>doubling of data sample)
- error on $|V_{ub}/V_{cb}|$ of $\sim 5\%$
- error on γ : $\sim 10\text{-}15^\circ$? ($r_B \dots$)
- LHC-b will have initial data

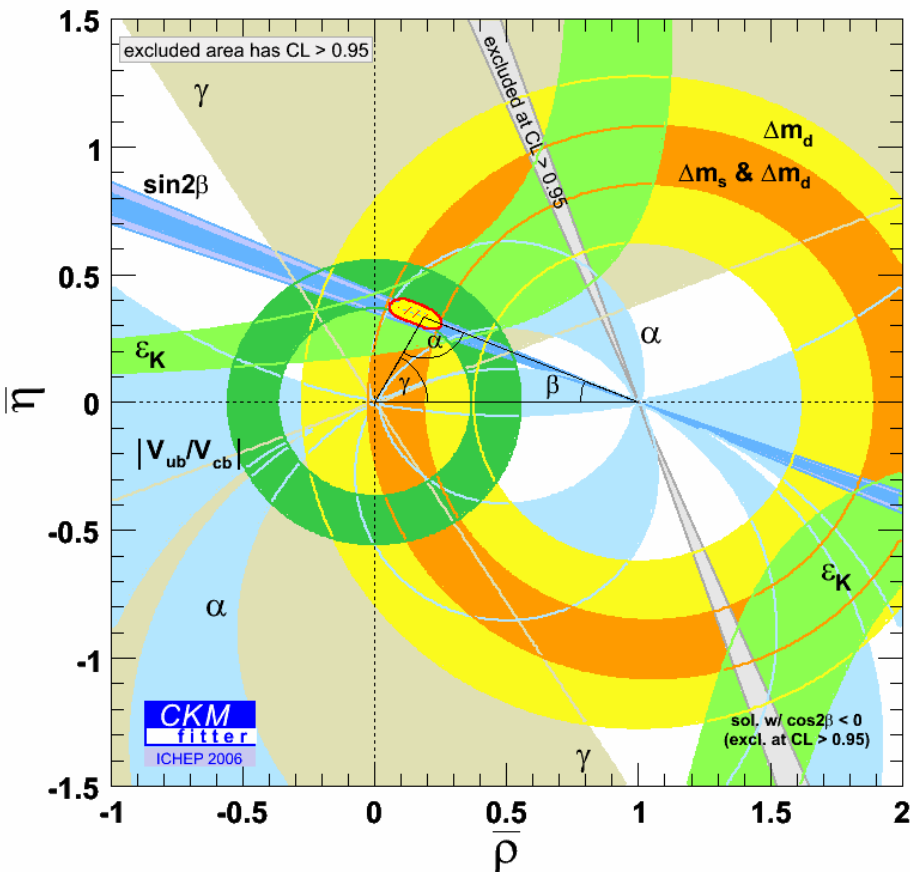
- The heavy flavor program will restrict the space in which theories for the new physics to be seen at LHC can operate



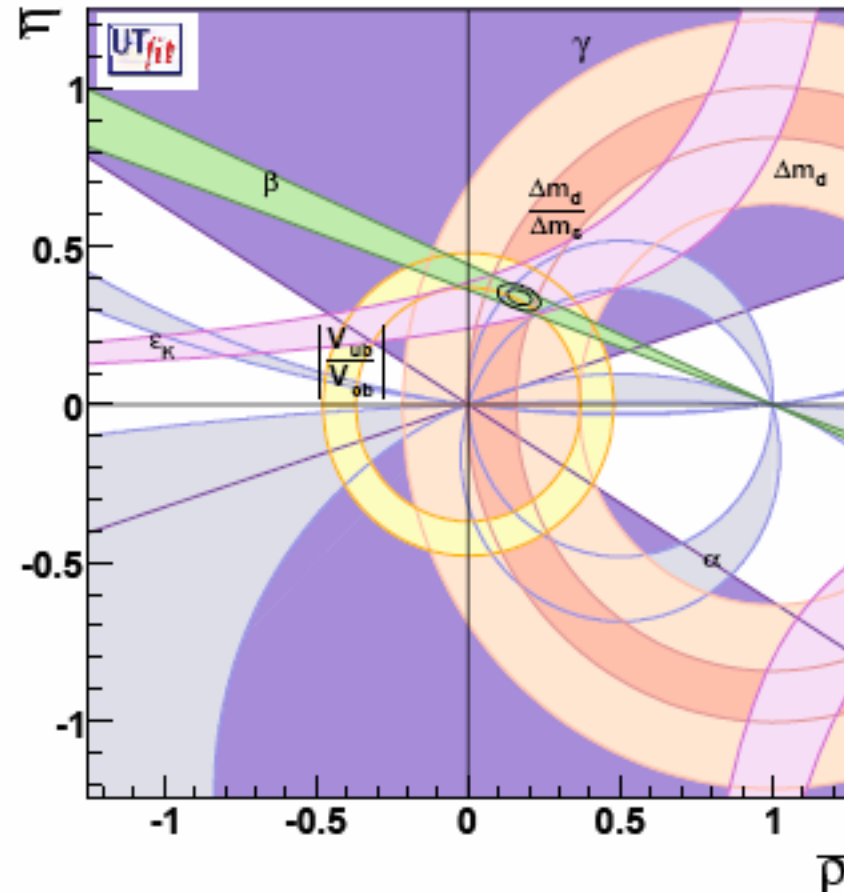
Backup slides

Tale of two fitters

CKMfitter (frequentist)



UTFit (Bayesian)



Theory calculations



- Bosch, Lange, Neubert, Paz (BLNP)
 - Decompose into Hard, Jet and Shape functions using HQE and SCET: $H \times J \times S$
 - Same formalism used to extract m_b and μ_π^2 from $b \rightarrow s\gamma$
 - Predictions over full phase space, reasonable error analysis
 - Critique: 3 scales between Λ_{QCD} and m_b
- Andersen and Gardi: Dressed gluon exponentiation (DGE)
 - Only m_b and α_s as input parameters
 - Gives good description of $b \rightarrow s\gamma$ spectrum
 - Agrees fairly well with BLNP on $b \rightarrow u\ell\nu$ rates
 - Critique: some (but not all) consider it a model;

Global fit: Input measurements



- Moments used in fit, from $B \rightarrow X_c \ell \nu$ and $b \rightarrow s \gamma$

**Buchmüller and Flücher,
Phys.Rev. D73 (2006) 073008**

\ Moment Experiment	Electron energy	Hadronic mass	Photon energy
Delphi	3	3	
CLEO	need full covar	4	1
CDF		2	
Belle	need full covar	need full covar	4
BaBar	14	13	3

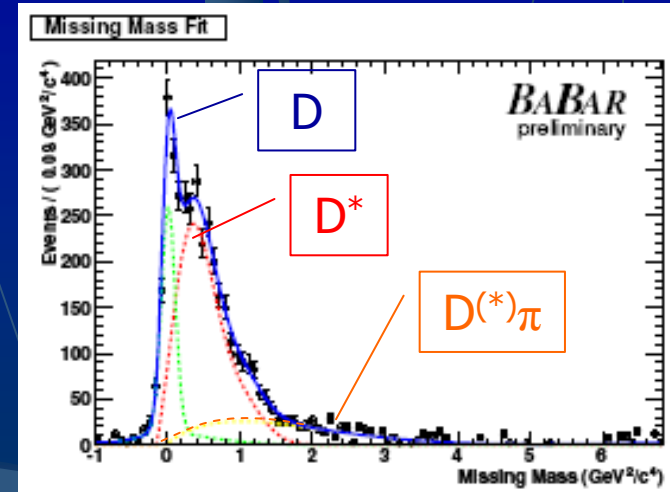
$B \rightarrow X_c \ell \bar{\nu}$ using tagged samples

- Reconstruct $D^{(*)} X \ell \bar{\nu}$ across from a fully reconstructed B^+ or B^0 meson; M_{miss}^2 provides new kinematic handle
- Belle reported last year
BFs for $B \rightarrow D^{(*)} \pi \ell \bar{\nu}$:
Phys.Rev.D72:051109,2005

$D^+ \pi^- \ell^- \bar{\nu}_\ell$	Belle BF (in %)	$0.54 \pm 0.07 \pm 0.07 \pm 0.06$
$D^{*+} \pi^- \ell^- \bar{\nu}_\ell$		$0.67 \pm 0.11 \pm 0.09 \pm 0.03$
$D^0 \pi^+ \ell^- \bar{\nu}_\ell$		$0.33 \pm 0.06 \pm 0.06 \pm 0.03$
$D^{*0} \pi^+ \ell^- \bar{\nu}_\ell$		$0.65 \pm 0.12 \pm 0.08 \pm 0.05$

Also report $\text{BF}(B^- \rightarrow D^{*0} \ell^- \bar{\nu}) = 6.06 \pm 0.25_{\text{stat}}\%$;
and $\text{BF}(B^0 \rightarrow D^{*+} \ell^- \bar{\nu}) = 4.70 \pm 0.24_{\text{stat}}\%$.

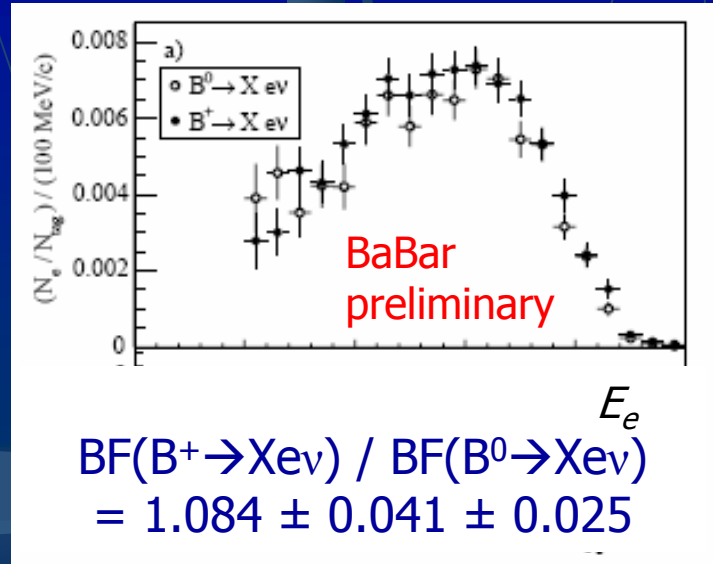
- New BaBar preliminary result:
 $\text{BF}(B^- \rightarrow D^{*0} \ell^- \bar{\nu}) = 6.8 \pm 0.4\%$
 $\text{BF}(B^- \rightarrow D^0 \ell^- \bar{\nu}) = 2.3 \pm 0.3\%$
 $\text{BF}(B^- \rightarrow D^{*0} \ell^- \bar{\nu}) = 1.9 \pm 0.3\%$
(includes $D^{(*)} \pi \ell \bar{\nu}$; translated from relative fractions into BFs by this speaker assuming these modes saturate $b \rightarrow c \ell \bar{\nu}$)
- New D0 result (preliminary)
 $\text{BF}(B_s \rightarrow D_{s1}(2536) \ell \bar{\nu}) = 0.86 \pm 0.16 \pm 0.16$



The $BF(B \rightarrow D^* \ell \nu)$ puzzle

- The largest B BF is $B \rightarrow D^* \ell \nu$ ($\sim 6\%$), yet $B \rightarrow K^* \gamma$ ($\sim 4 \times 10^{-5}$) is known as well, and perhaps better...
- (HFAG winter) average: $BF(\underline{B}^0 \rightarrow D^{*+} \ell^- \nu) = 5.35 \pm 0.20\%$; CL=3.8%
- Consider $R_{D^*} = BF(B^- \rightarrow D^{*0} \ell^- \nu) / BF(\underline{B}^0 \rightarrow D^{*+} \ell^- \nu)$;
we expect $R_{D^*} = \tau_+ / \tau_0 = 1.071 \pm 0.009$
- Naively combining Belle and BaBar results: $R_{D^*} = 1.32 \pm 0.07$
(20% and 3.5σ from isospin!)

Total $BF(B \rightarrow X \ell \nu)$
consistent with isospin



Importance of r_B

- The uncertainty on γ (φ_3) depends strongly on the value of r_B , which is currently not well known
- Predictions for how σ_γ will evolve with luminosity have significant uncertainty

